

# Massive MIMO in 5G Wireless Networks

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(MBNRG)

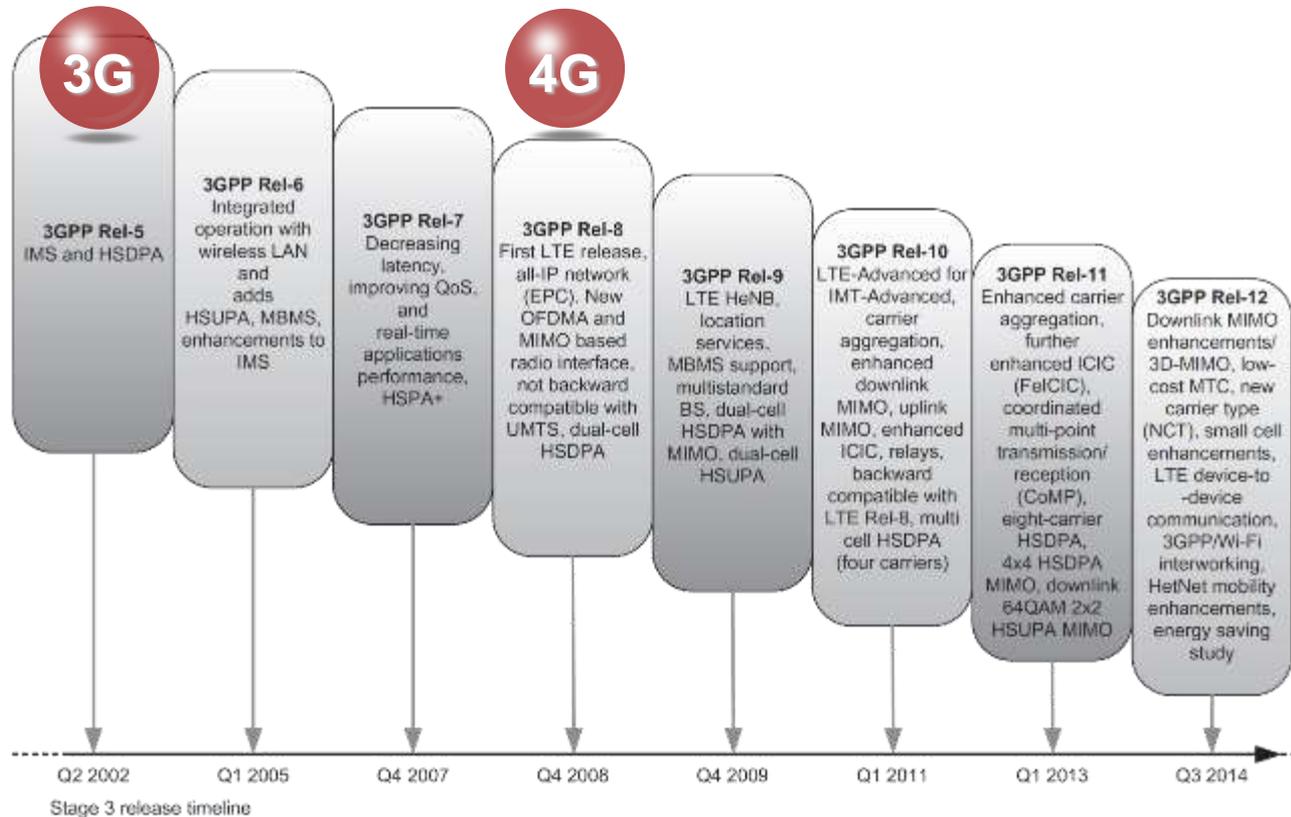
Iran University of Science and Technology (IUST)

# An Introduction to 5G



[www.mobilebroadband.ir](http://www.mobilebroadband.ir)

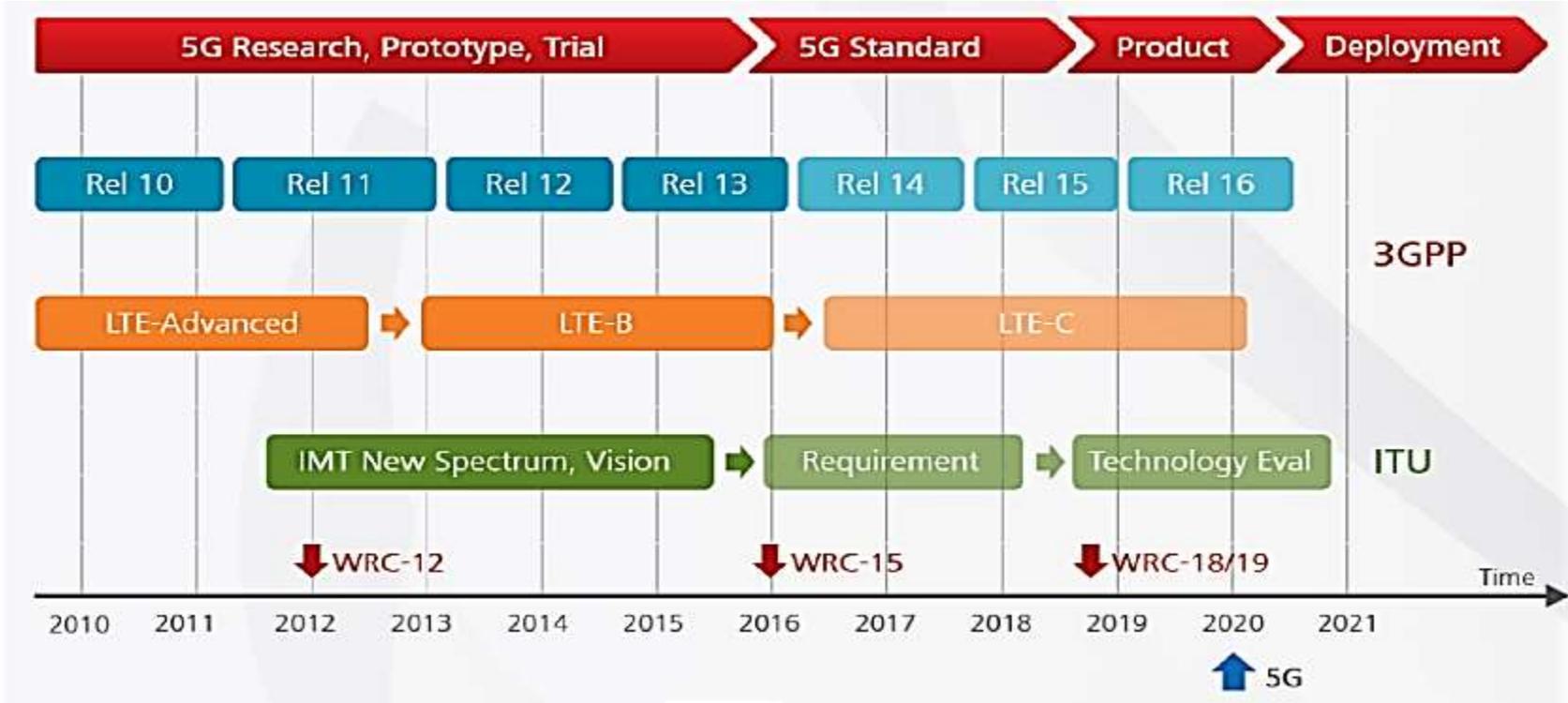
# Evolution of Wireless Networks



1980   1990

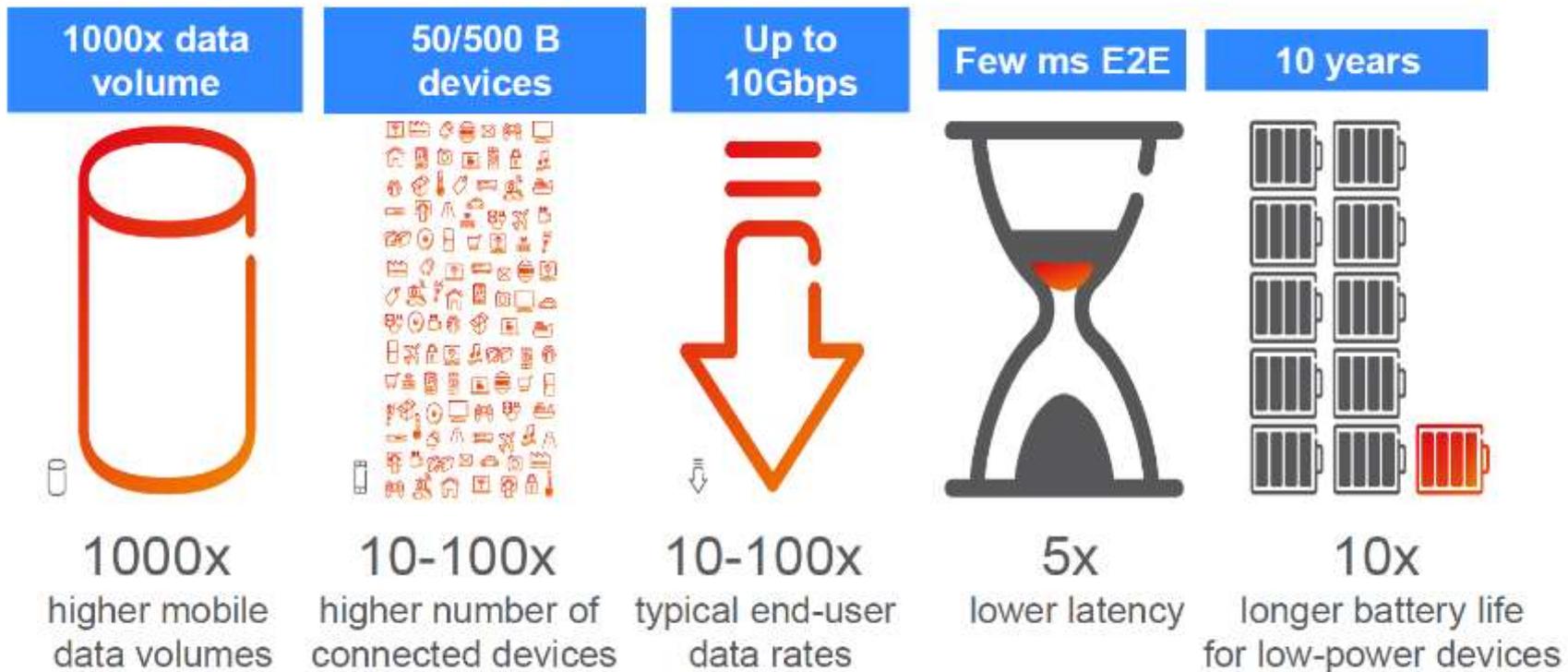
2020

# 5G Timeline



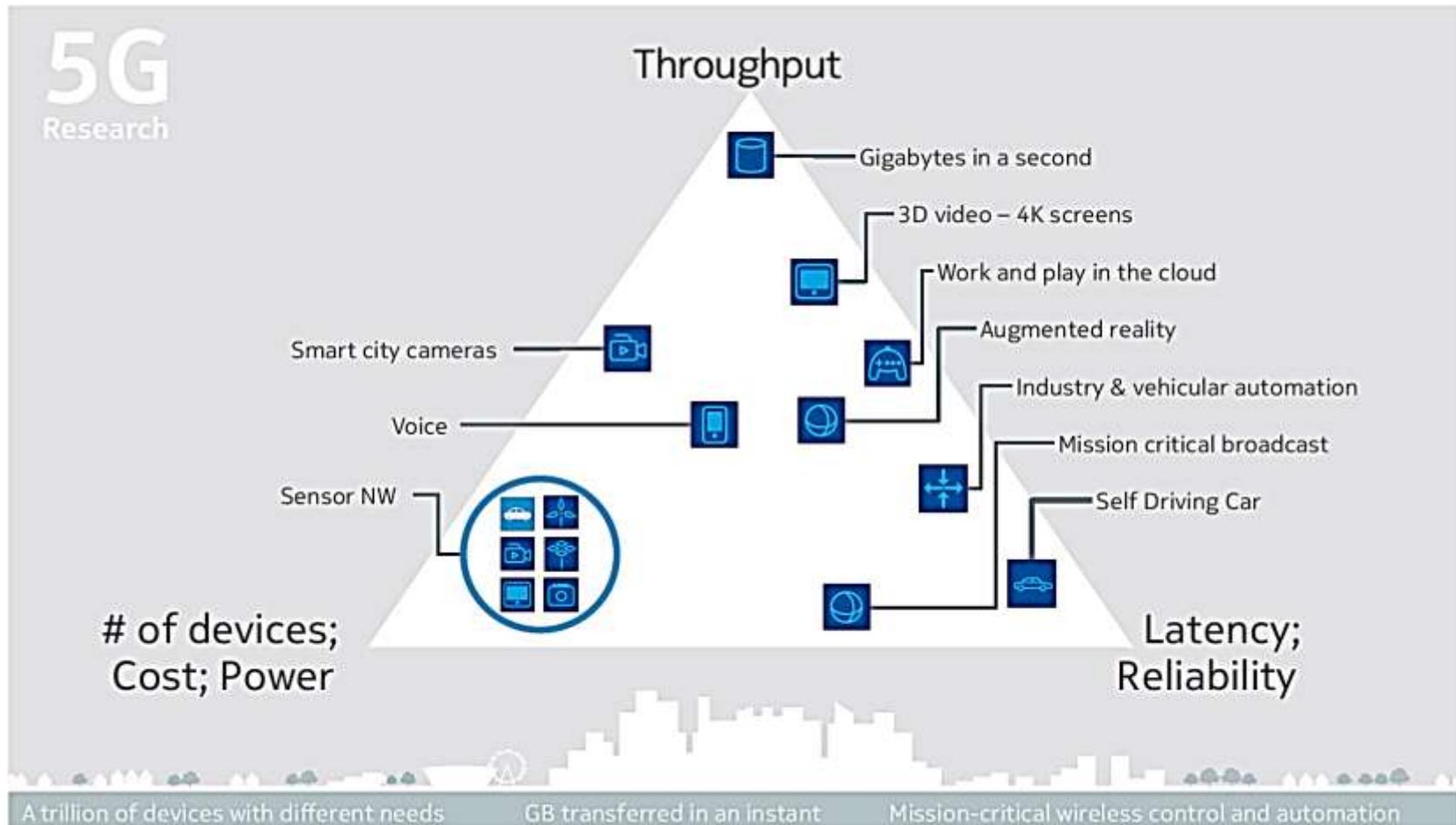
Ref: Huawei 2015

# 5G Objectives



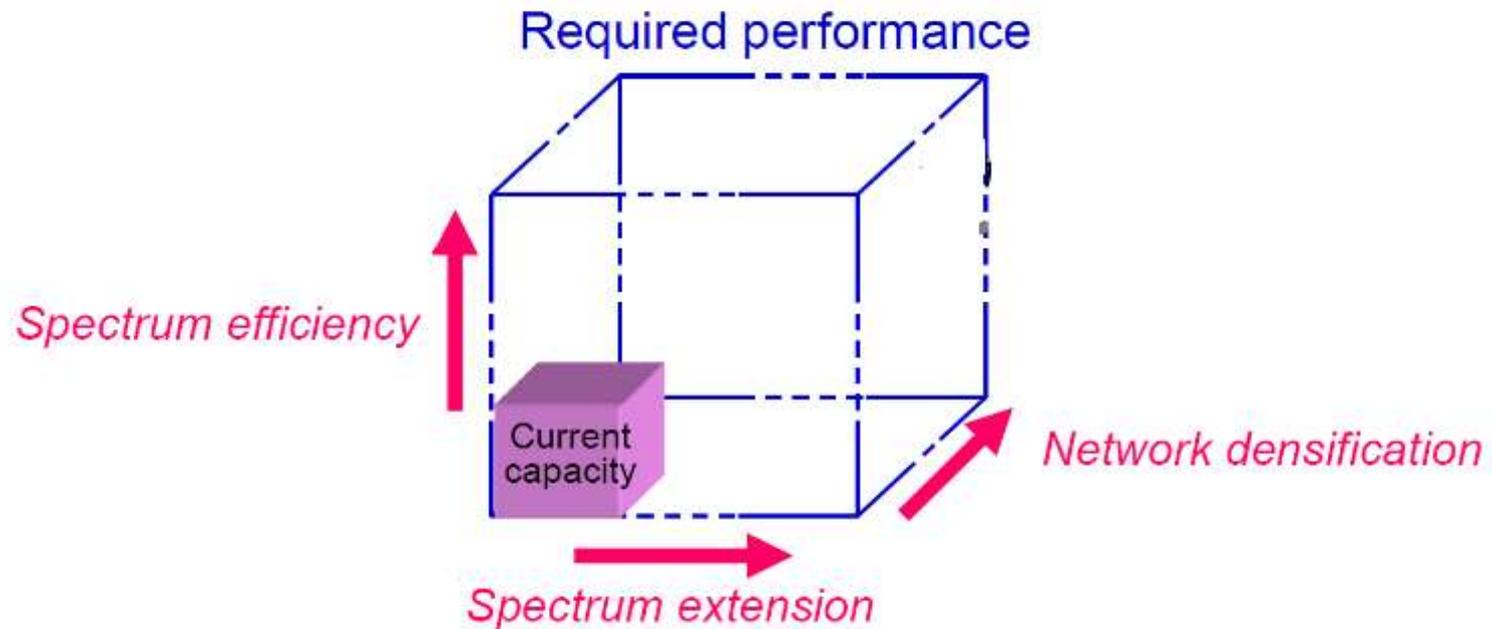
Ref: ITU

# 5G Use Cases

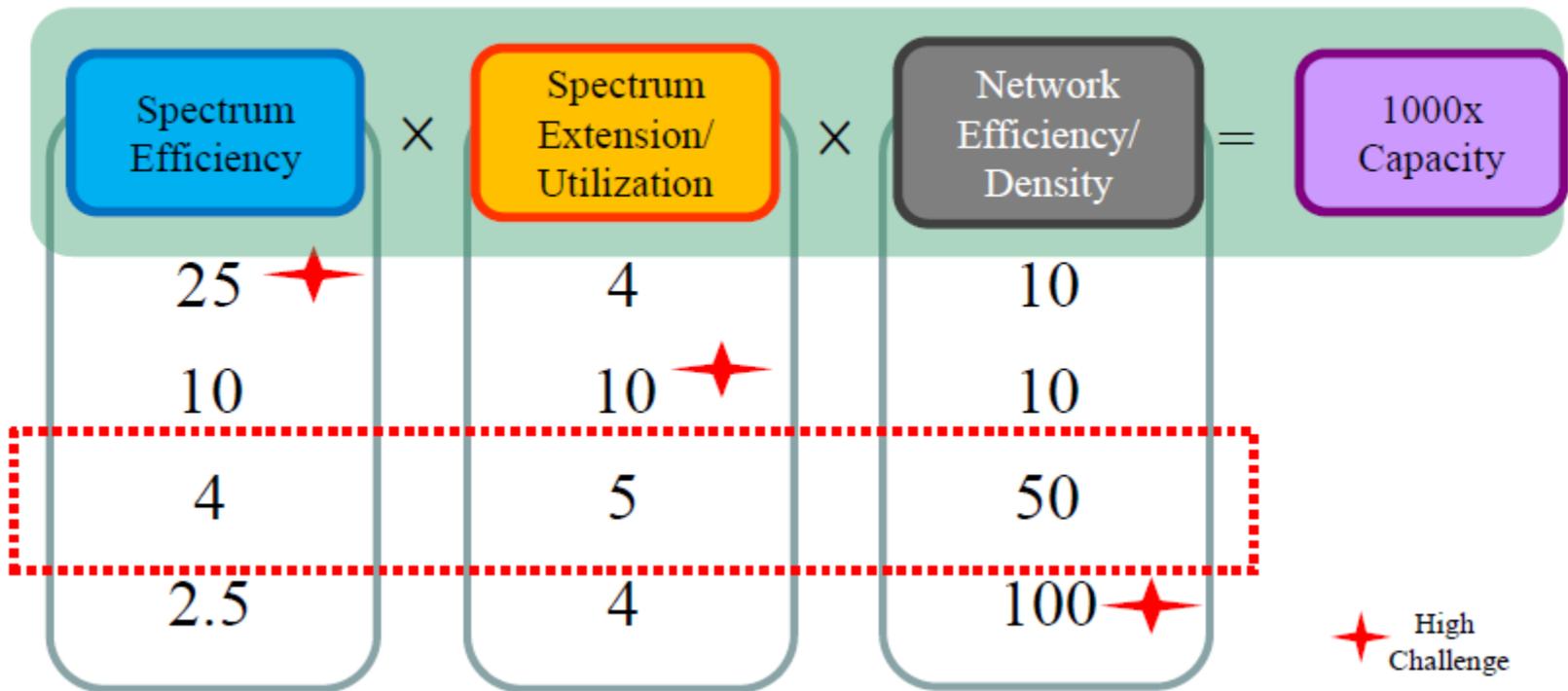


Ref: Nokia

# 5G Radio Access Solutions

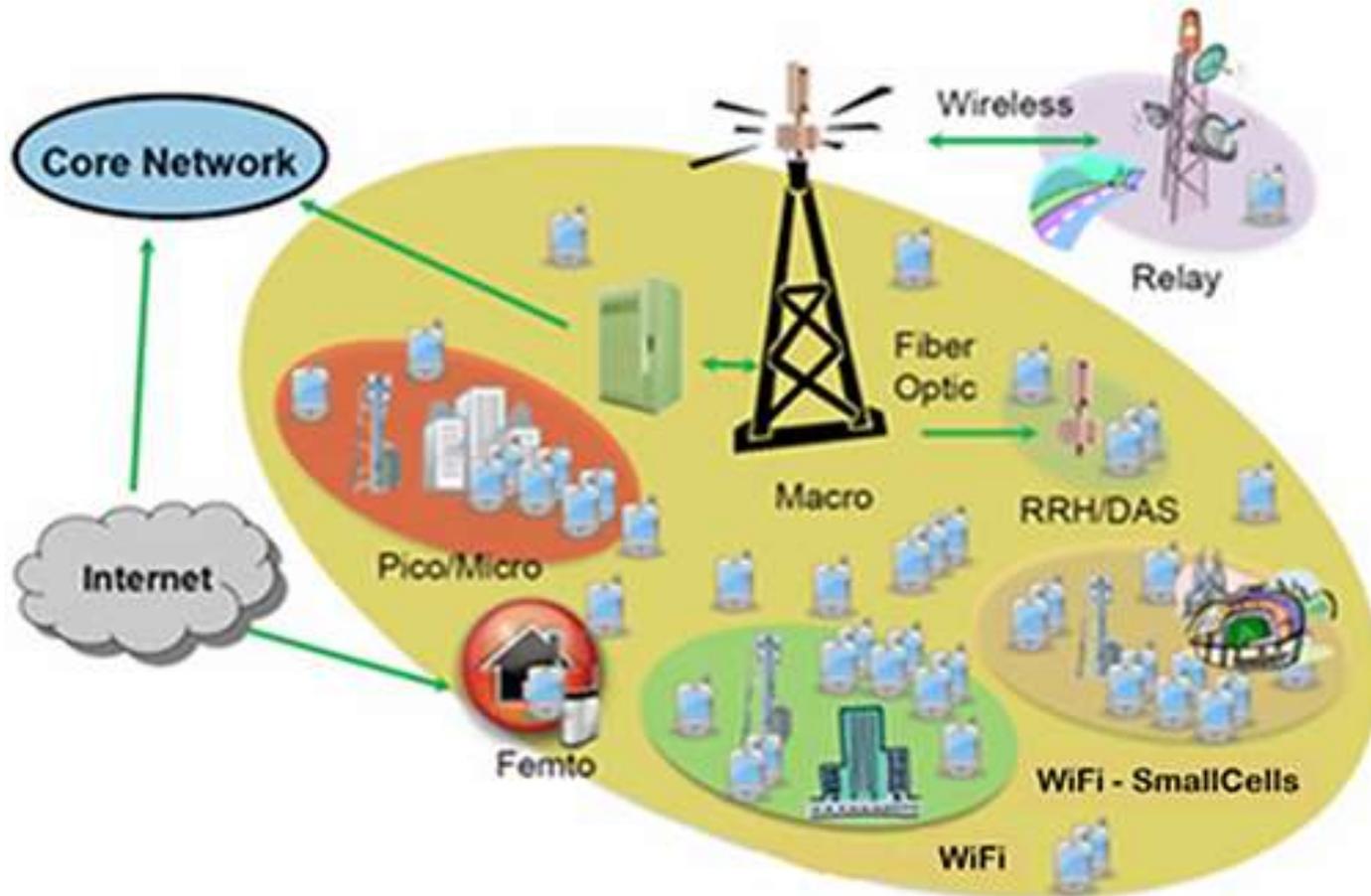


# 5G Radio Access Technologies



# Network densification

HetNet



Ref: Tutorial @ ICC 2014

# Spectrum Extension

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- Higher frequencies and millimeter waves
- New Regulations
- Unlicensed bands
- Spectrum Aggregation
- Spectrum Sharing
- Cognitive radio

# mmWave

- 30 to 300 GHz
  - 23, 29, 38, 40, 46, 47, 49GHz, and E-band
- Already used in LAN, PAN, and VANET
  - backhaul in cellular networks

Frequency range	6-20 GHz	20-40 GHz	40-60 GHz	60-100 GHz
Specific bands identified	<i>10 GHz band</i> 10.125-10.225 GHz / 10.475-10.575 GHz	<i>32 GHz band</i> 31.8-33.4 GHz	<i>40 GHz band</i> 40.5-43.5 GHz  <i>'45 GHz' band</i> 45.5-48.9 GHz	<i>66 GHz band</i> 66-71 GHz
Potential bandwidth	<i>2 x100 MHz</i>	<i>1.6 GHz</i>	<i>5.8 GHz total</i>	<i>5 GHz</i>



# mmW

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- Advantages
  - Higher BW
  - Multi-Gbps data rate
  - Less interference --> intra-tier and inter-tier
  - Dense spectrum re-use
  - Compact equipment
  - Spatial multiplexing

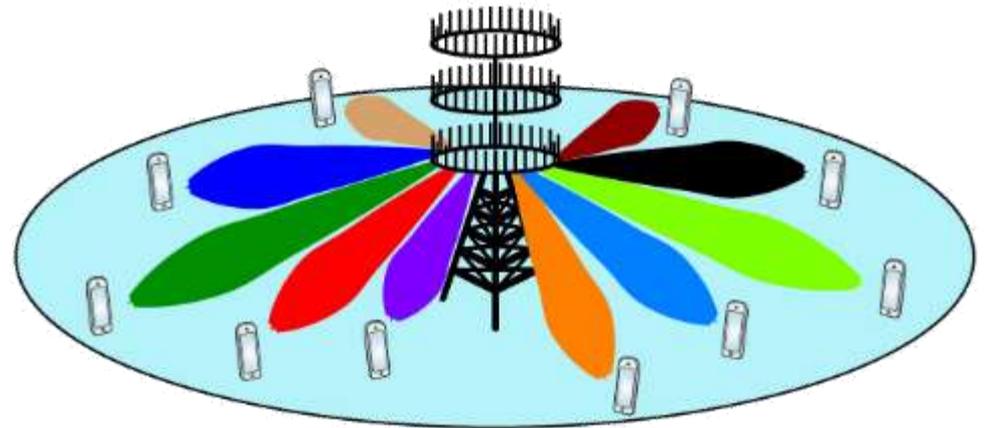
# Other technologies in 5G

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- Software based architecture (SDN and NFV)
- Radio Access Technologies:
  - In-band full duplex
  - Non-orthogonal multiple access (NOMA)
  - Filter-bank multicarrier (FBMC)
  - Three dimensional beamforming
  - **Massive MIMO**

# Massive MIMO

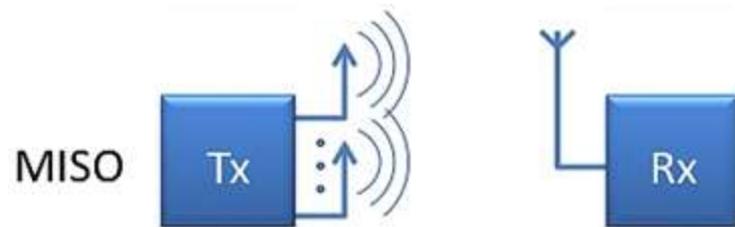
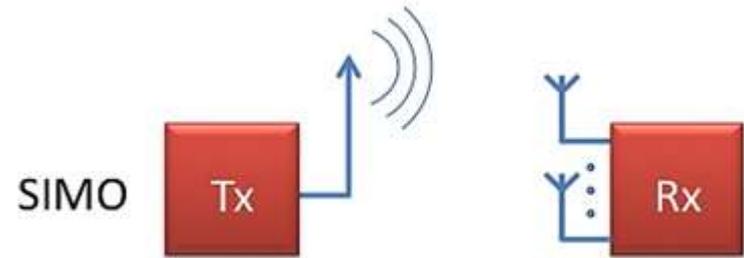
- Large-scale antenna systems
- Employing a large number of antennas at the BS
- High spectral efficiency
- High energy efficiency
- Simpler processing



**Introduction to  
Massive  
MIMO**



# Multiple Antenna Systems



# Multiple Antenna Advantages

Spectral efficiency

Diversity and link reliability

Space-Time Coding

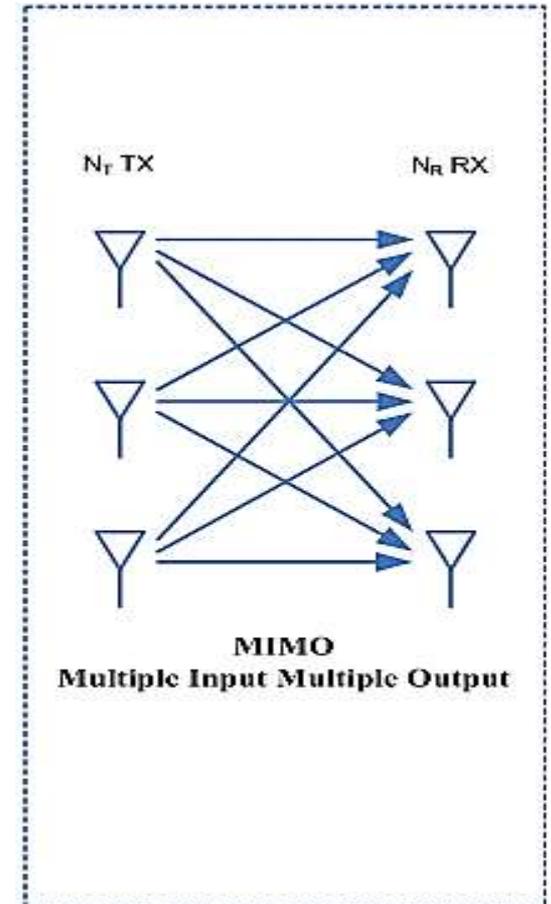
V-BLAST

Precoding (Beamforming)

Diversity Gain

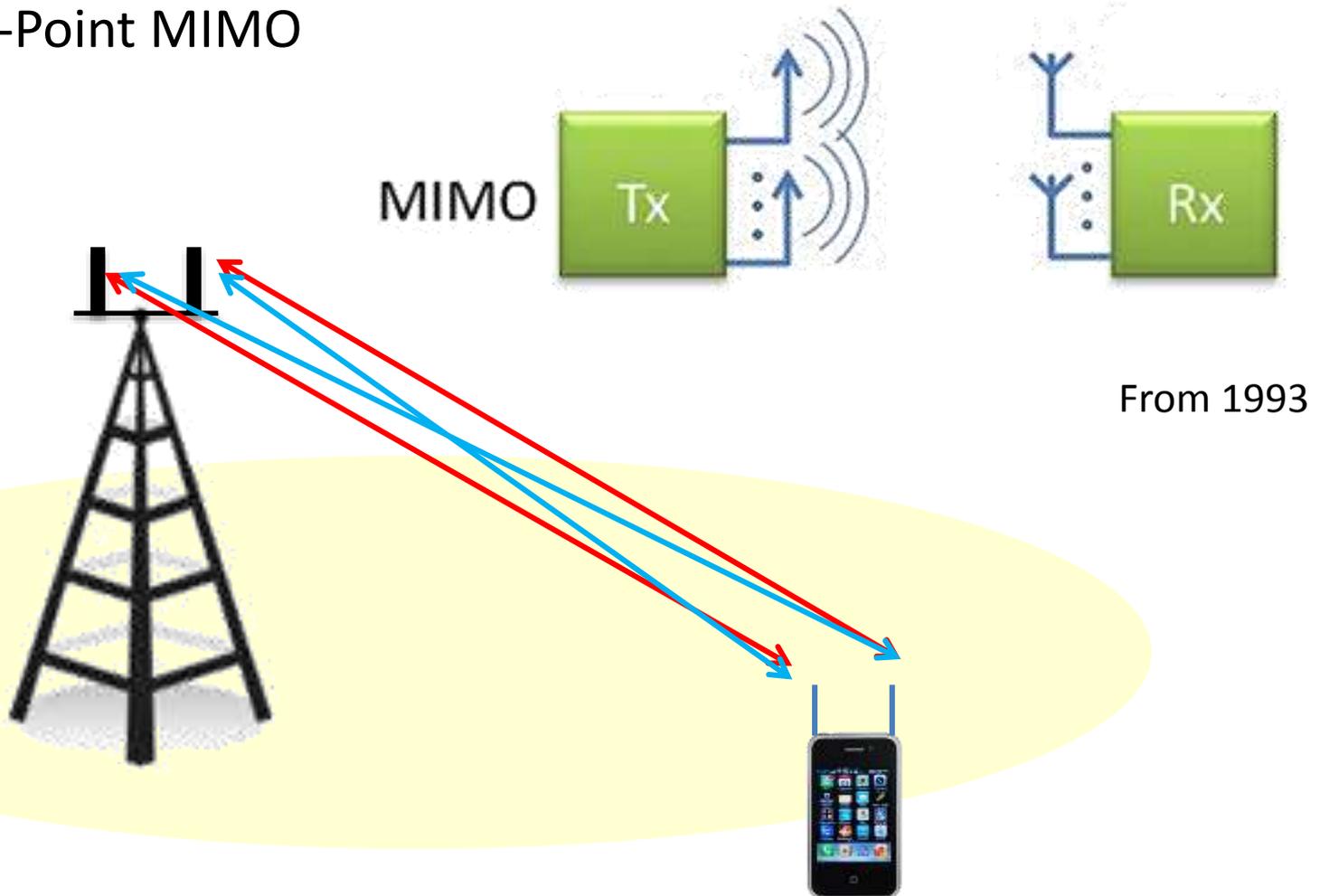
Multiplexing Gain

Array Gain



# Single-User MIMO

- Point-to-Point MIMO



# Single-User MIMO

- $N_t \times N_r$  MIMO system
- Received signal



$$\mathbf{y} = \sqrt{\rho} \mathbf{H} \mathbf{x} + \mathbf{n},$$

- Capacity (iid channels)

$$C = \log_2 \det \left( \mathbf{I} + \frac{\rho}{N_t} \mathbf{H} \mathbf{H}^H \right)$$

# Single-User MIMO

- With normalized channel

$$\text{Tr}(\mathbf{H}\mathbf{H}^H) \approx N_t N_r$$



- Upper and lower bound

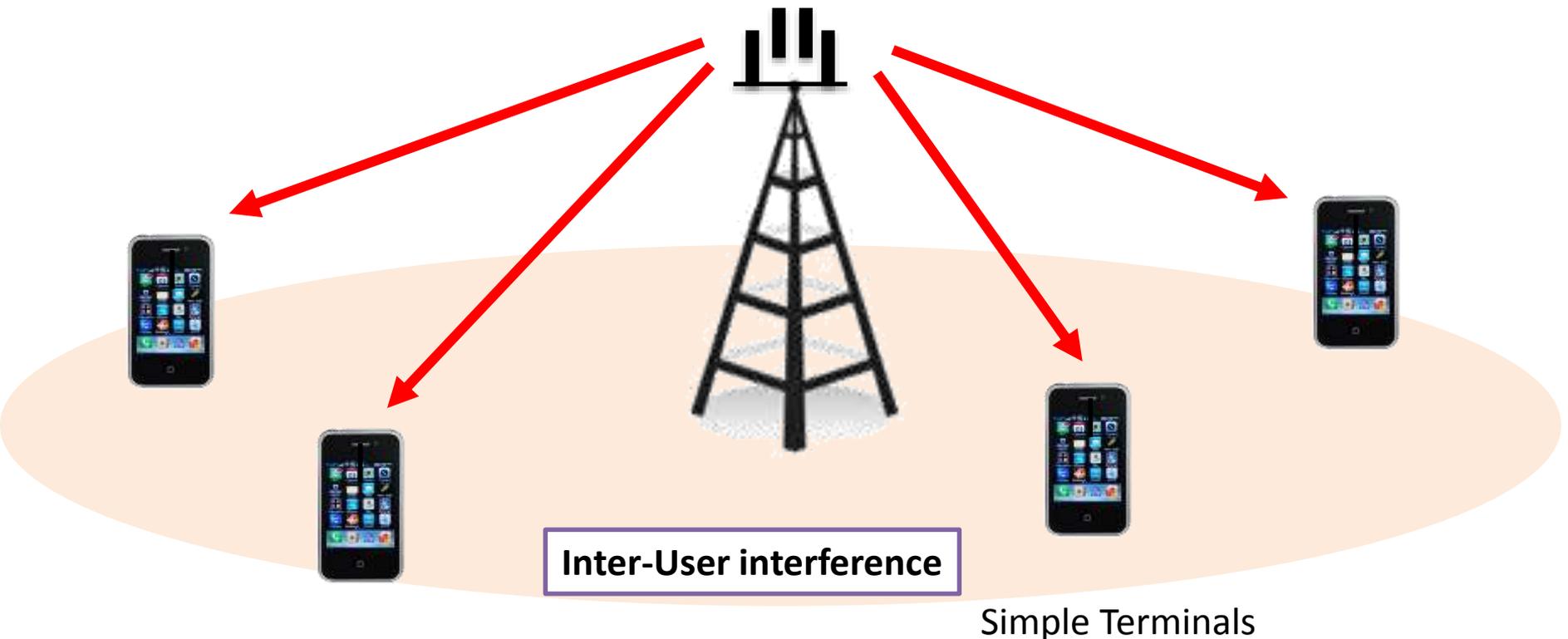
$$\log_2(1 + \rho N_r) \leq C \leq \min(N_t, N_r) \log_2 \left( 1 + \frac{\rho \max(N_t, N_r)}{N_t} \right)$$

- Problems of SU-MIMO:
  - Unfavorable propagations
  - Low multiplexing gain at cell edge

Lu Lu, et.al, "An overview of massive MIMO: Benefits and challenges," IEEE J. Sel. Topics Signal Process., Oct. 2014.

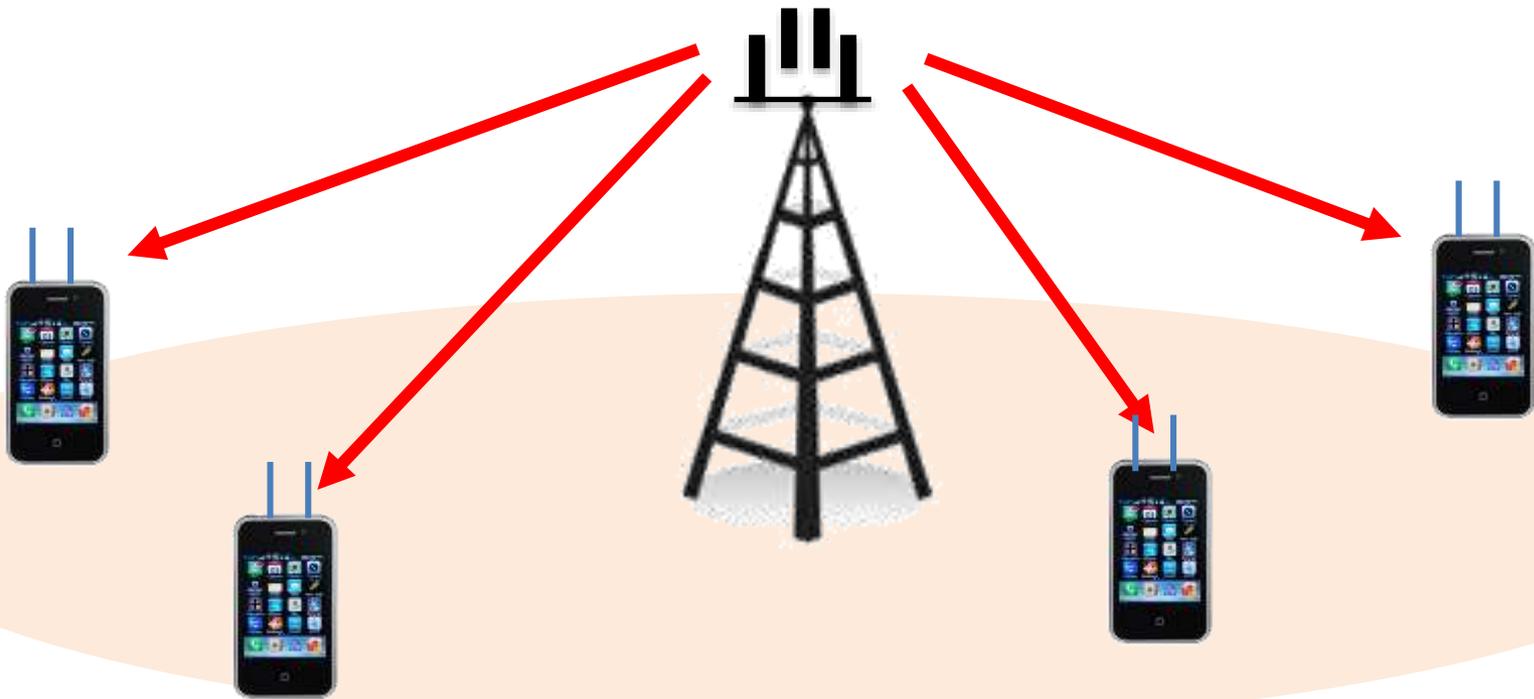
# Multi-user MIMO

- multiple data streams to multiple single antenna users



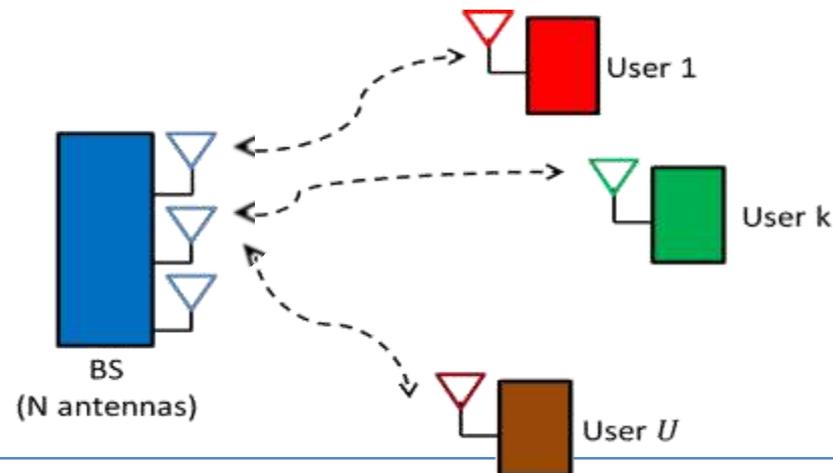
# MU-MIMO

- Multiple Antenna Users



# MU-MIMO

- MU-MIMO categories
  - MIMO broadcast channels (MIMO BC) – DL
    - Precoding: Linear and Non-Linear, ZF, MMSE, BD, DPC, THP, VP
  - MIMO multiple access channels (MIMO MAC) - UL
    - Decoding: Linear and Non-Linear, ZF, MMSE, ML



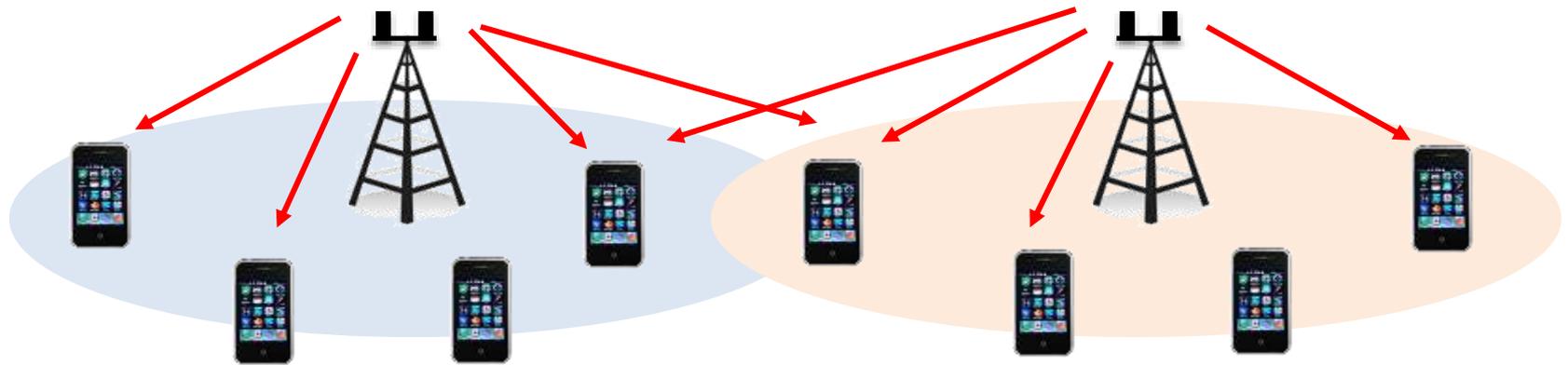
# MU-MIMO

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- More immune to most of propagation limitations
  - Channel rank loss or antenna correlation
  - Effect of the line-of-sight (LOS) propagation
- Development of small and cheap terminals
  - Single-antenna users
- Different techniques
  - SDMA, massive MIMO, coordinated multipoint (CoMP), Ad-hoc MIMO

# MIMO Categories

- Multi-cell MIMO
  - Network MIMO



Inter-cell interference (ICI)

# MU-MIMO

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- **Challenges in the practice**
- Limited number of antennas at the BS (LTE-A)
- User scheduling
  - Selection of a group of users that will be served simultaneously
    - Max-rate techniques , Random user selection
- Channel state information at transmitter (CSIT) in DL
  - Vector quantization , Adaptive feedback , Statistical feedback
- Coordination of BSs

# Conventional MIMO System

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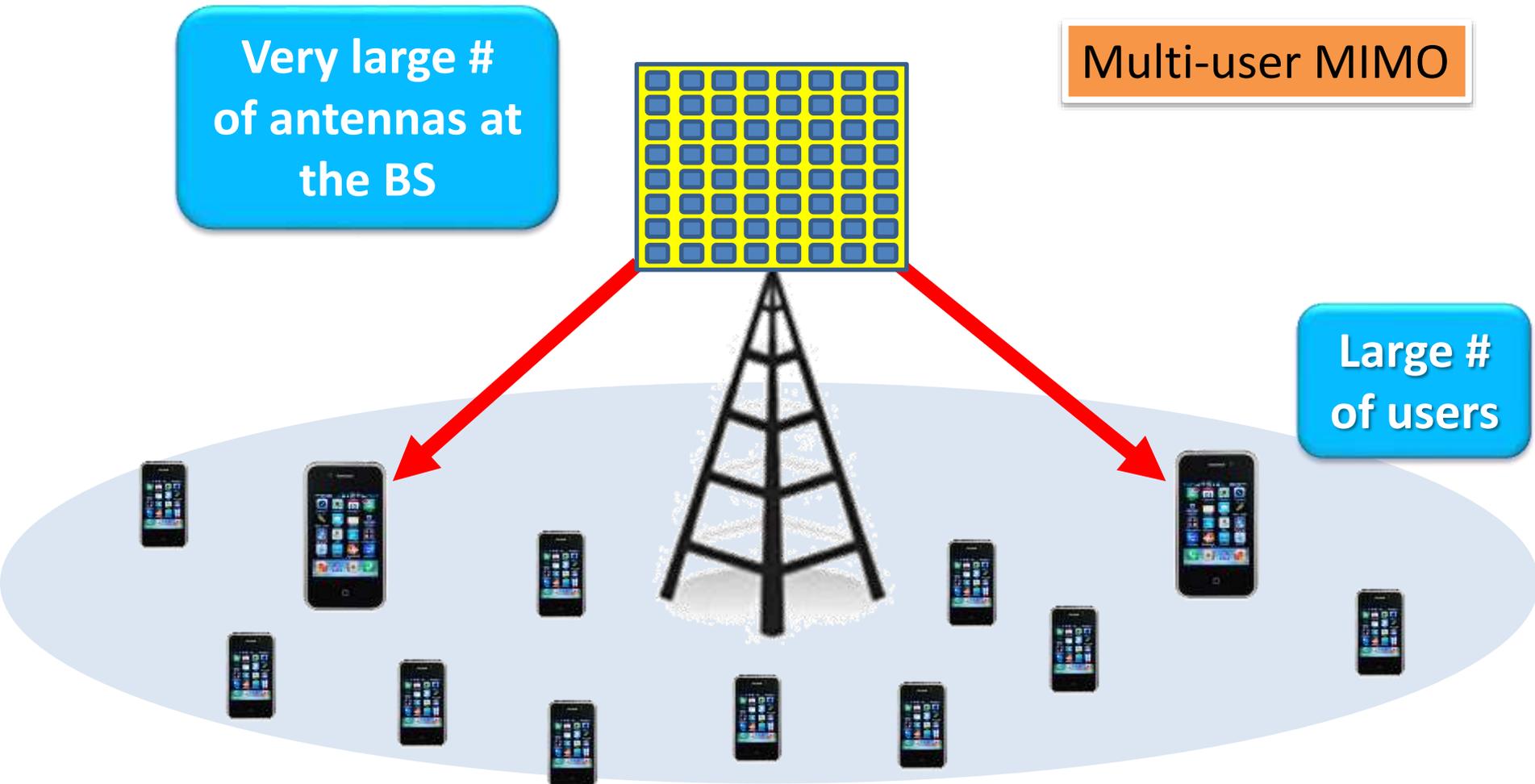
- Few # of Antenna at the BS
- Antenna ports – Antenna Elements
  - UMTS: 3 sectors x 20 element-arrays = 60 antennas
  - LTE-A: 4-MIMO x 60 = 240 antennas
- 4x4 or 8x8
- SU-MIMO
- **AAS** – Active Antenna Systems

# Massive MIMO

Very large #  
of antennas at  
the BS

Multi-user MIMO

Large #  
of users



# Massive MIMO

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3590

IEEE TRANSACTIONS ON WIRELESS COMMUNICATIONS, VOL. 9, NO. 11, NOVEMBER 2010

## Noncooperative Cellular Wireless with Unlimited Numbers of Base Station Antennas

Thomas L. Marzetta



# Massive MIMO

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- General assumptions:
  - CSI is only available at the BS
  - Linear precoding/decoding
  - No signal processing at users
- Benefits
  - Very narrow beams
  - Less Interference leakage
  - Simplicity
  - Higher Energy efficiency
  - Higher Spectral efficiency

# Advantages of Massive MIMO

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**High spectral efficiency**

**Lower transmit power**

**High energy efficiency**

**Simple processing (MF)**

**Higher capacity**

**Extended Range**

**Higher reliability**

**More degrees of freedom (interference nulling)**

**Simplified resource allocation and power control**

**Better tradeoff Spectral – energy efficiency**

**Good service for all users in the cell**

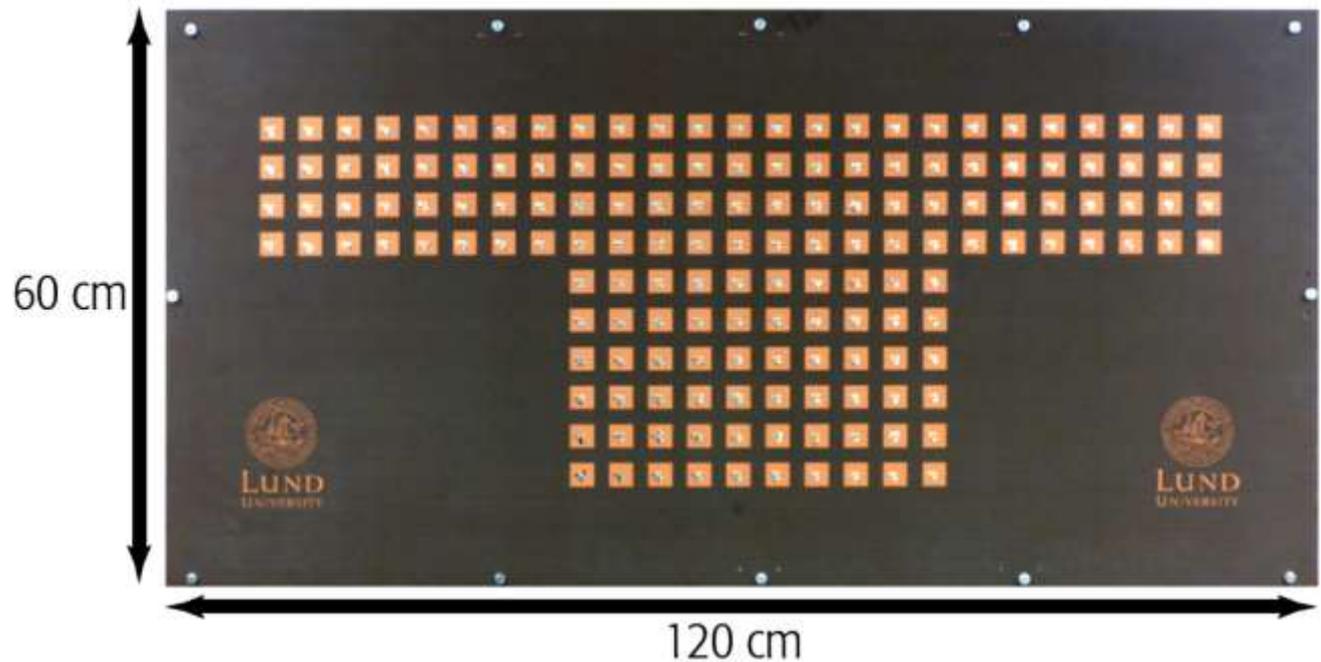
# Example

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- Example (Marzeta'2010)
  - **MF**, non-cooperative
  - 42 users
  - 20 MHz BW
  - 17 Mbps for each user (both UL and DL)
  - Average 730 Mbps per cell
  - Overall Spectral efficiency : 36.5 bps/Hz

# Example

- LuMaMi testbed, Lund University
- 160 antennas



- Many antenna ports

# Asymptotic Analysis (single user)

- $N_t \gg N_r$  and  $N_t \rightarrow \infty$

$$C = \log_2 \det \left( \mathbf{I} + \frac{\rho}{N_t} \mathbf{H} \mathbf{H}^H \right)$$

$$\frac{(\mathbf{H} \mathbf{H}^H)}{N_t} \approx \mathbf{I}_{N_r}$$

- Achievable rate

$$C \approx N_r \log_2(1 + \rho)$$

- Upper bound is achieved

$$\min(N_t, N_r) \log_2 \left( 1 + \frac{\rho \max(N_t, N_r)}{N_t} \right)$$

# Asymptotic Analysis (single user)

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- $N_r \gg N_t$  and  $N_r \rightarrow \infty$

$$\frac{(\mathbf{H}\mathbf{H}^H)}{N_r} \approx \frac{N_r}{N_t} \mathbf{I}_{N_t}$$

- Achievable rate

$$C \approx N_t \log_2 \left( 1 + \frac{\rho N_r}{N_t} \right)$$

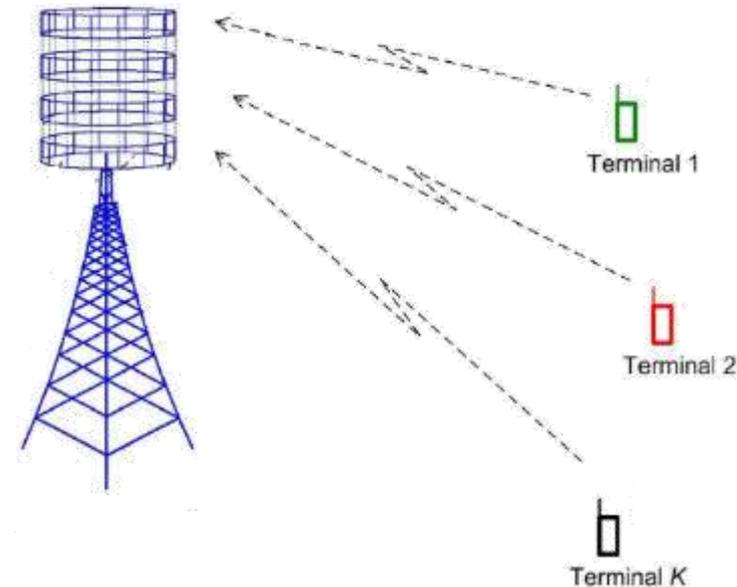
- **Upper bound is achieved**  $\min(N_t, N_r) \log_2 \left( 1 + \frac{\rho \max(N_t, N_r)}{N_t} \right)$
- Column or rows of H need to be orthogonal = not in LOS (favorable propagation)

# Asymptotic Analysis (Multi-user)

- BS with  $N$  antennas and  $K$  users
- Uplink: received signal

$$\mathbf{y}_u = \sqrt{\rho_u} \mathbf{H} \mathbf{x}_u + \mathbf{n}_u$$

- Where  $\mathbf{H} = \mathbf{G} \mathbf{D}^{1/2}$



# Asymptotic Analysis (Multi-user)

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- Independent fading channels for different users
- When  $N \rightarrow \infty$

$$\mathbf{H}^H \mathbf{H} = \mathbf{D}^{1/2} \mathbf{G}^H \mathbf{G} \mathbf{D}^{1/2} \approx N \mathbf{D}^{1/2} \mathbf{I}_K \mathbf{D}^{1/2} = N \mathbf{D}$$

- Sum rate of the cell (network)

$$\begin{aligned} C &= \log_2 \det(\mathbf{I} + \rho_u \mathbf{H}^H \mathbf{H}) \approx \log_2 \det(\mathbf{I} + N \rho_u \mathbf{D}) \\ &= \sum_{k=1}^K \log_2(1 + N \rho_u d_k) \end{aligned}$$

# Asymptotic Analysis (Multi-user)

- Simple **MF** Processing (UL)

$$\mathbf{H}^H \mathbf{y}_u = \mathbf{H}^H (\sqrt{\rho_u} \mathbf{H} \mathbf{x}_u + \mathbf{n}_u) \approx N \sqrt{\rho_u} \mathbf{D} \mathbf{x}_u + \mathbf{H}^H \mathbf{n}_u$$

- No inter-user interference !

White noise

- Like a SISO channel

- SNR of each user  $N \rho_u d_k$

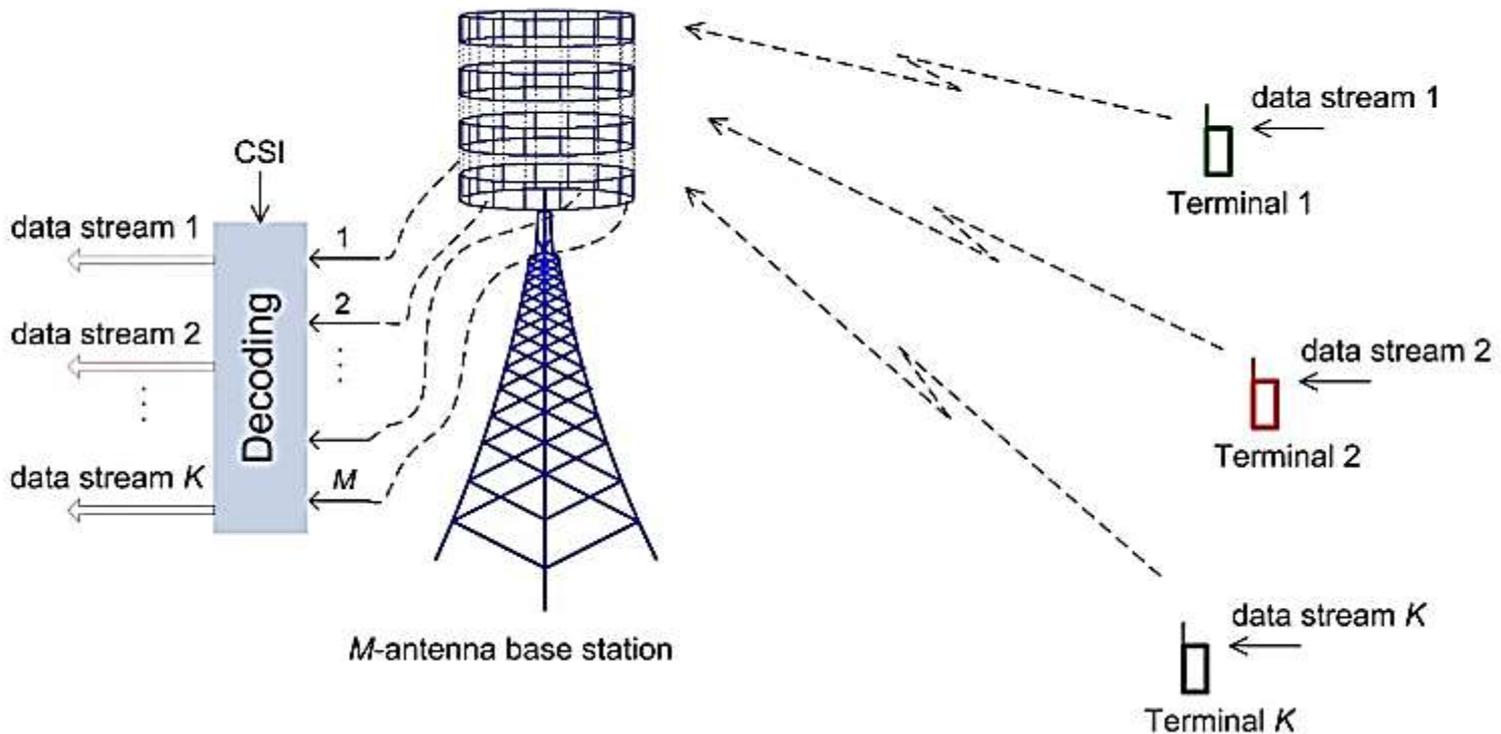
- The capacity is achieved by MF

- MF is optimal !

$$\sum_{k=1}^K \log_2(1 + N \rho_u d_k)$$

# Asymptotic Analysis (Multi-user)

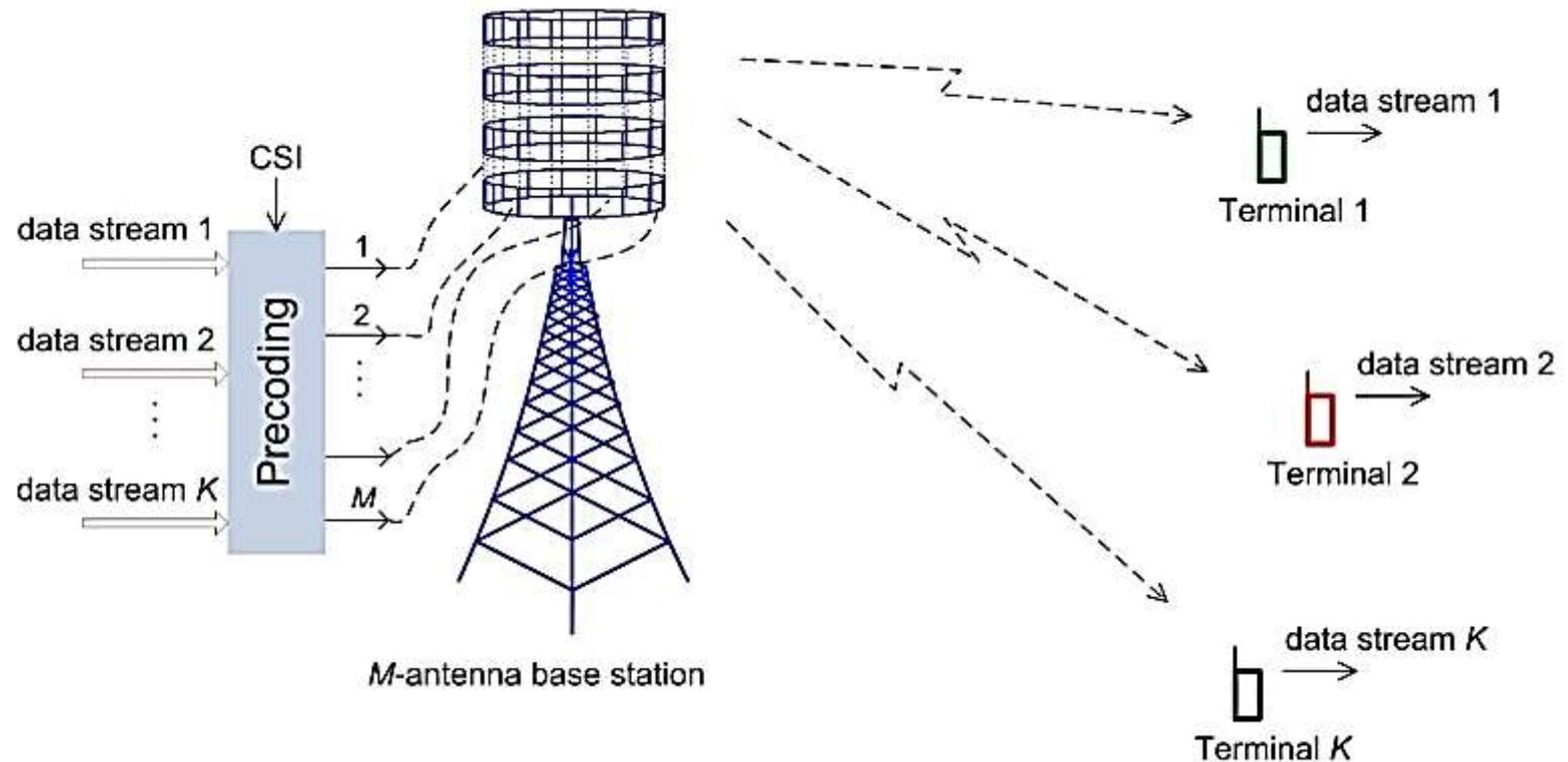
- Uplink



Thomas L. Marzetta "MASSIVE MIMO: FUNDAMENTALS AND SYSTEM ISSUES", Lund Circuit Design Workshop, Sep. 2015

# Asymptotic Analysis (Multi-user)

- Downlink



Thomas L. Marzetta " MASSIVE MIMO: FUNDAMENTALS AND SYSTEM ISSUES" , Lund Circuit Design Workshop , Sep. 2015

# Asymptotic Analysis (Multi-user)

- Downlink:
- Received signal vector at all K users  $\mathbf{y}_d = \sqrt{\rho_d} \mathbf{H}^T \mathbf{x}_d + \mathbf{n}_d$
- TDD mode and CSI knowledge
- CSIT  $\rightarrow$  Power allocation can be used at the BS for max. rate

$$C = \max_{\mathbf{P}} \log_2 \det(\mathbf{I}_N + \rho_d \mathbf{H} \mathbf{P} \mathbf{H}^H) \approx \max_{\mathbf{P}} \log_2 \det(\mathbf{I}_K + \rho_d N \mathbf{P} \mathbf{D})$$

- Power allocation matrix:  $\mathbf{P} = \text{diag}(p_1, p_2, \dots, p_K)$ ,  $\sum_1^K p_k = 1$

S. Vishwanath et.al., "Duality, achievable rates, and sum-rate capacity of Gaussian MIMO broadcast channels," IEEE Trans. Inf. Theory, Oct. 2003.

Lu Lu, et.al, "An overview of massive MIMO: Benefits and challenges," IEEE J. Sel. Topics Signal Process., Oct. 2014.

# Asymptotic Analysis (Multi-user)

- Using MF precoder

$$\mathbf{x}_d = \mathbf{H}^* \mathbf{D}^{-1/2} \mathbf{P}^{1/2} \mathbf{s}_d$$

- The received vector

$$\mathbf{y}_d = \sqrt{\rho_d} \mathbf{H}^T \mathbf{H}^* \mathbf{D}^{-1/2} \mathbf{P}^{1/2} \mathbf{s}_d + \mathbf{n}_d$$

- $N \rightarrow \infty$

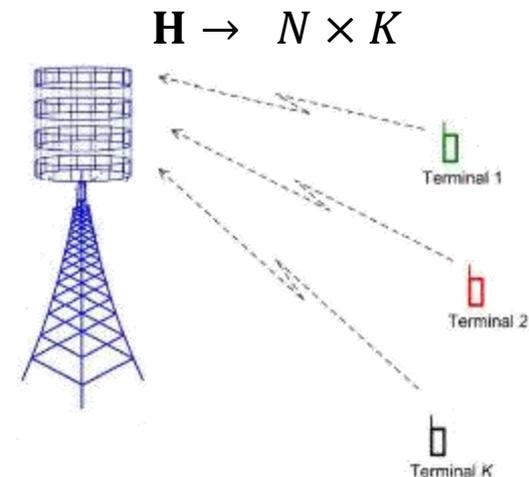
$$\mathbf{y}_d \approx \sqrt{\rho_d} N \mathbf{D}^{1/2} \mathbf{P}^{1/2} \mathbf{s}_d + \mathbf{n}_d$$

- No inter-user interference !
- **Capacity can be achieved by MF precoder** (Optimal powers)

# Channel Estimation

- Need for CSI : multiuser precoding (DL) or detection (UL)
- Pilot based channel estimation
- Preamble 

Pilot	Data
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- In general, time and freq. resources required for estimation is proportional to the # of TR antennas
- Two modes of operation: **FDD** and **TDD**



# Channel Estimation

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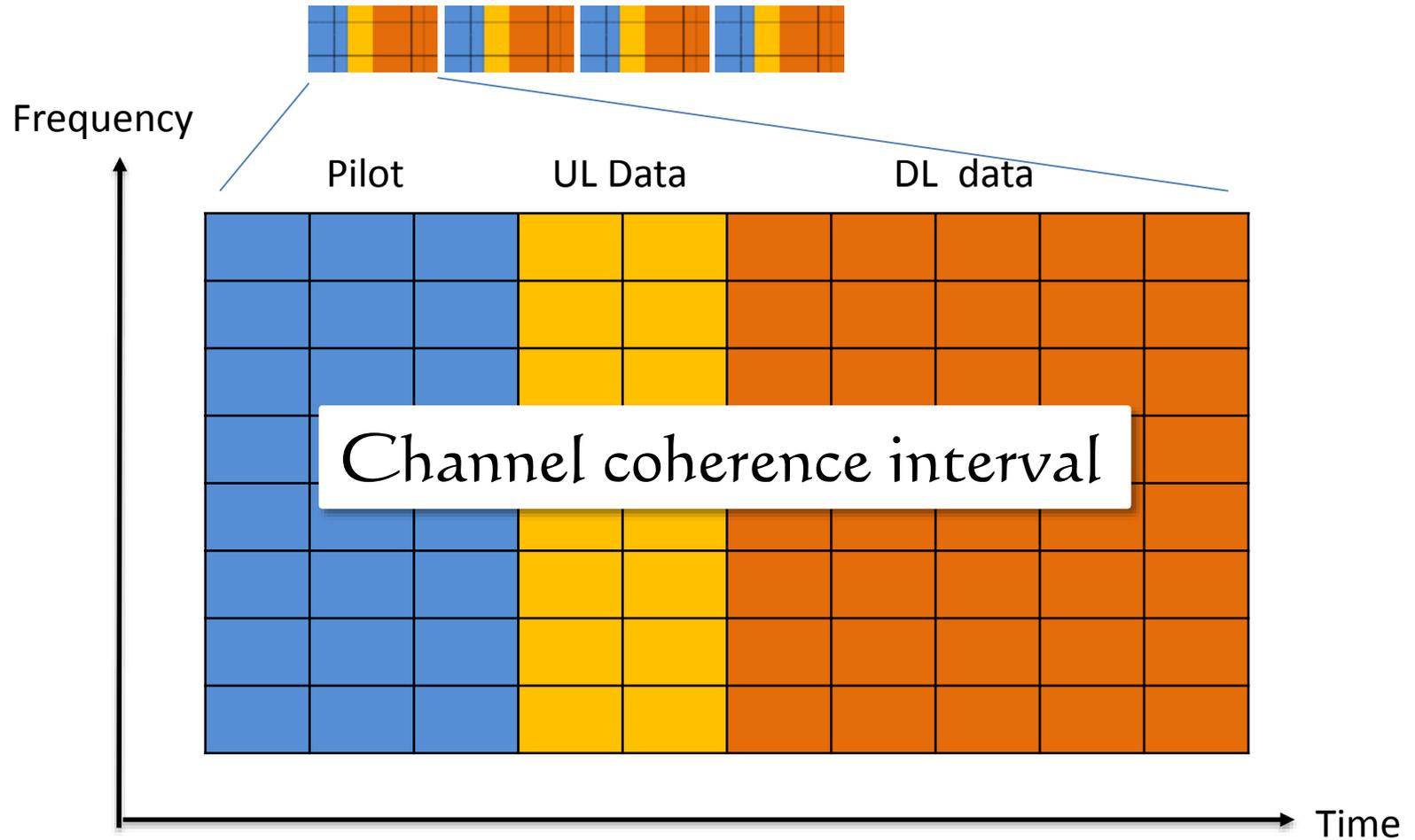
- **FDD**: Different CSI in UL and DL
  - no reciprocity in the channel
- Uplink → No problem
- Downlink → A big challenge
- BS transmits pilot symbols
- Channel estimation at the users
- Pilot length is proportional to the # of the BS antennas
- In large # of BS antenna ( $N$ ) → FDD is infeasible
  - Whole coherence interval is used for pilot transmission

# Channel Estimation

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- **TDD**
- Channel reciprocity
- Uplink pilot and channel estimation
- Pilot length is proportional to the # of the users (K)
  - Independent of N
  - $N \rightarrow \infty$

# Channel Estimation



# Pilot Contamination

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- Pilot assignment in multi-cell networks
- Limitation in Pilots length ==> # of orthogonal pilots
- Pilot reusing
- Non-orthogonal pilots in neighbor cells
- **Interference !**

# Pilot Contamination

- Error in channel estimation
  - a linear combination of the channels with the same pilots

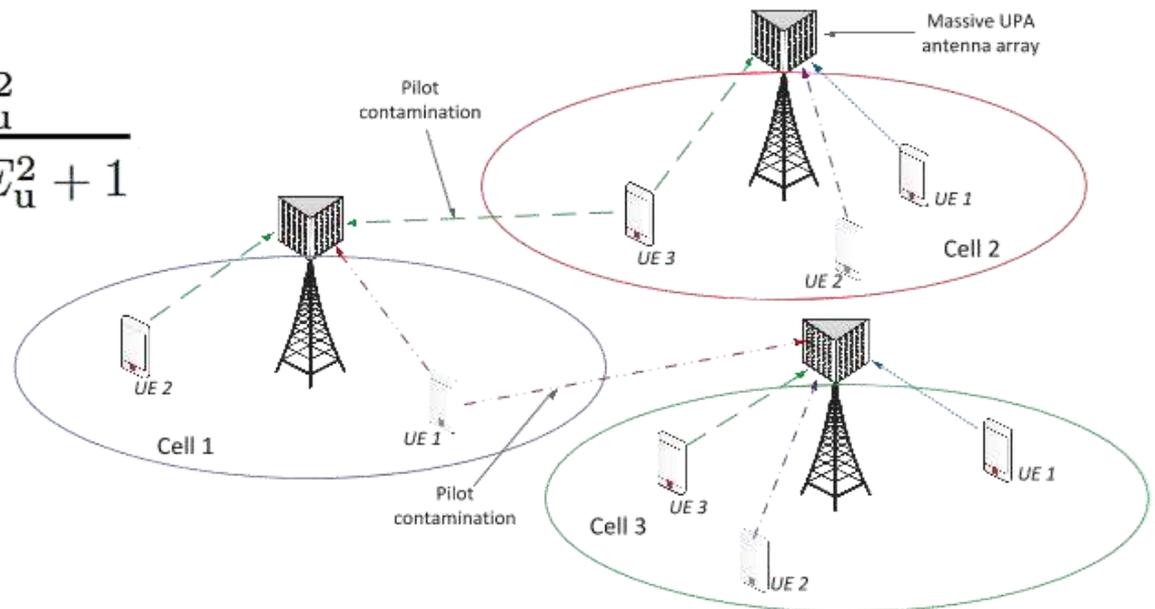
MMSE estimation  $\hat{\mathbf{H}}_{jl} = \sqrt{p_r \tau} \mathbf{D}_{jl}^{\frac{1}{2}} \mathbf{\Psi}_j^\dagger \left( \mathbf{I} + p_r \tau \sum_{i=1}^L \mathbf{\Psi}_i \mathbf{D}_{il} \mathbf{\Psi}_i^\dagger \right)^{-1} \mathbf{Y}_l$

$$\hat{\mathbf{H}}_i = \mathbf{H}_i + \sum_{j=1 \neq i}^L \mathbf{H}_{ij} + N$$

# Pilot Contamination

- Beamforming to users in other cells
- Not cancelled as  $N \rightarrow \infty$

$$\text{SINR}_{l,k}^{\text{IP}} \rightarrow \frac{\tau \beta_{lk}^2 E_u^2}{\tau \sum_{i \neq l}^L \beta_{lik}^2 E_u^2 + 1}$$



# Pilot Contamination

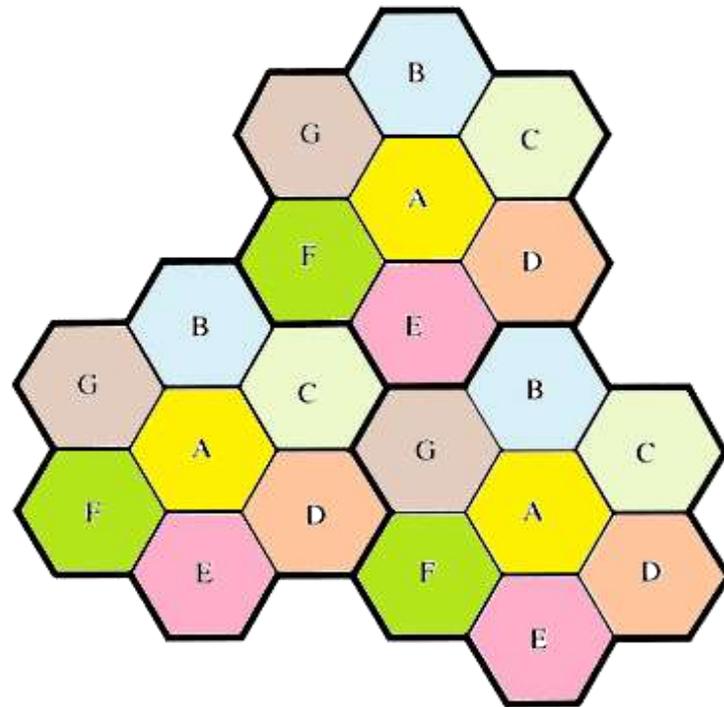
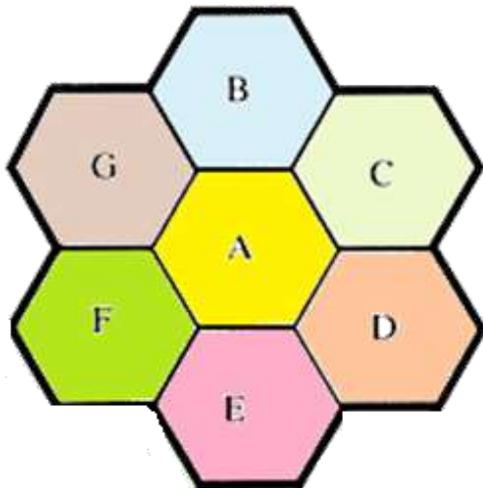
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- Main sources of pilot contamination
  - Non-orthogonal pilots
  - Hardware impairment
  - Non-reciprocal transceivers
- The final result

$$\text{SIR}_{rk} = \frac{\beta_{jkj}^2}{\sum_{l \neq j} \beta_{jkl}^2}$$

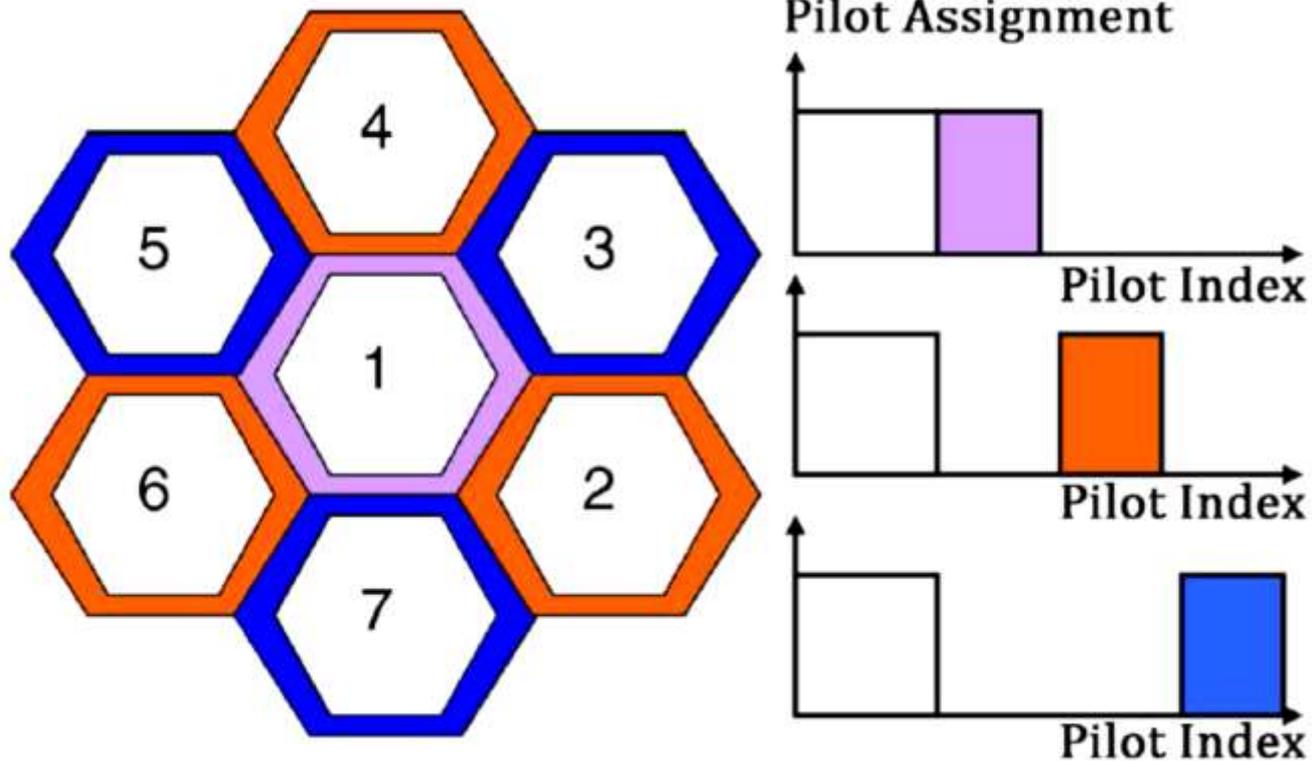
# Mitigation of Pilot Contamination

- Pilot partitioning and reusing



# Mitigation of Pilot Contamination

- Soft pilot reuse (SPR)



# Mitigation of Pilot Contamination

- Time shifted pilots



# Mitigation of Pilot Contamination

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- **Multi-cell cooperation based precoding**
  - Information exchange problem
  - In limited # of antennas
- **AoA-based methods**
- **Blind methods**
  - Sub-space partitioning
  - EVD-based estimation

# Signal Detection

- Linear detectors are near optimal

$$A = \begin{cases} G & \text{for MF} \\ G (G^H G)^{-1} & \text{for ZF} \\ G (G^H G + \frac{1}{p_u} I_K)^{-1} & \text{for MMSE} \end{cases}$$

$$\mathbf{r} = \sqrt{p_u} \mathbf{A}^H \mathbf{G} \mathbf{x} + \mathbf{A}^H \mathbf{n}$$

- ZF has better performance at high SNR
- Low complexity

# Energy Efficiency

- Spectral efficiency and Energy efficiency

$$EE = \frac{\sum_{k=1}^K \left( \mathbb{E} \left\{ R_k^{(ul)} \right\} + \mathbb{E} \left\{ R_k^{(dl)} \right\} \right)}{P_{TX}^{(ul)} + P_{TX}^{(dl)} + P_{CP}}$$

- Power scaling law

- Perfect CSI: proportional to  $N$

- Imperfect CSI: proportional to  $\sqrt{N}$

- $N \rightarrow \infty$  and same sum-rate as single antenna

$$SE = \sum_{k=1}^K \left( 1 - \frac{B}{T} \right) \log_2(1 + \text{SINR}_k)$$

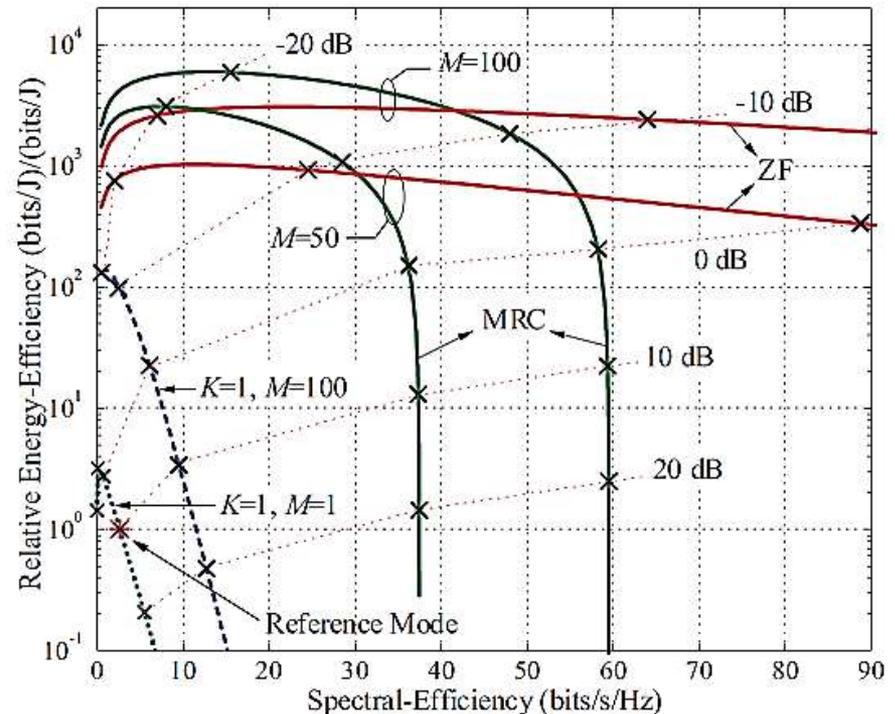
- Range extension

- Spectral Efficiency  $\times K$

H. Q.Ngo, E.G.Larsson, and T. L.Marzetta, "Energy and spectral efficiency of very large multiuser MIMO systems," *IEEE Trans. Commun.*, vol. 61, no. 4, pp. 1436–1449, Apr. 2013

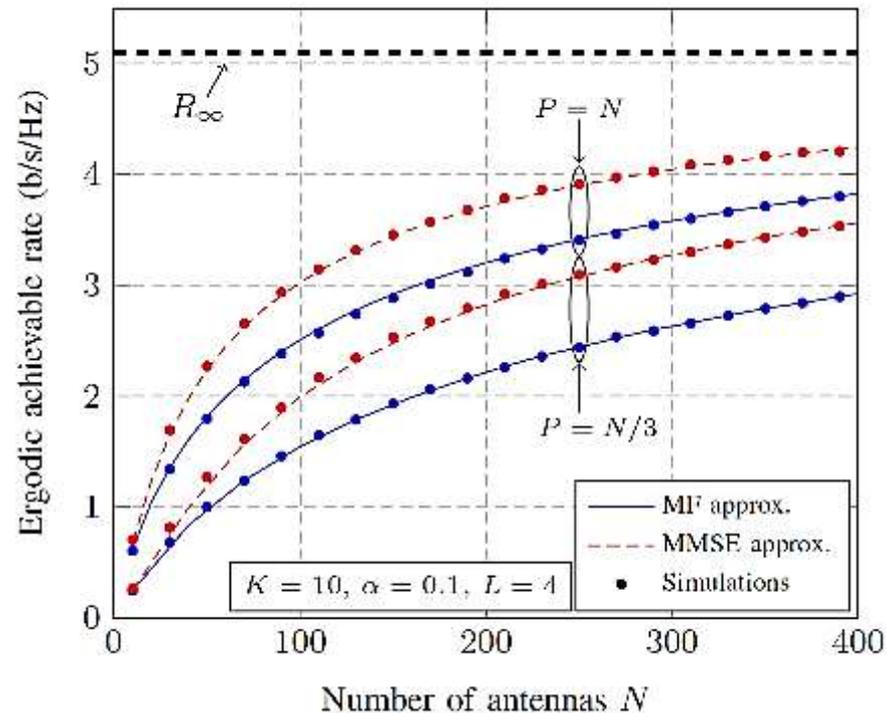
# Energy Efficiency

- Tradeoff of two efficiencies
  - Good in low SNRs
  - MRC and ZF with imperfect CSI
- Circuit power consumption !



# How many antennas do we need?

- In theory, more antenna ==> Better performance
- $N \rightarrow \infty$  ???



J. Hoydis et.al, "Massive MIMO in the UL/DL of cellular networks: How many antennas do we need?" IEEE JSAC Feb. 2013.

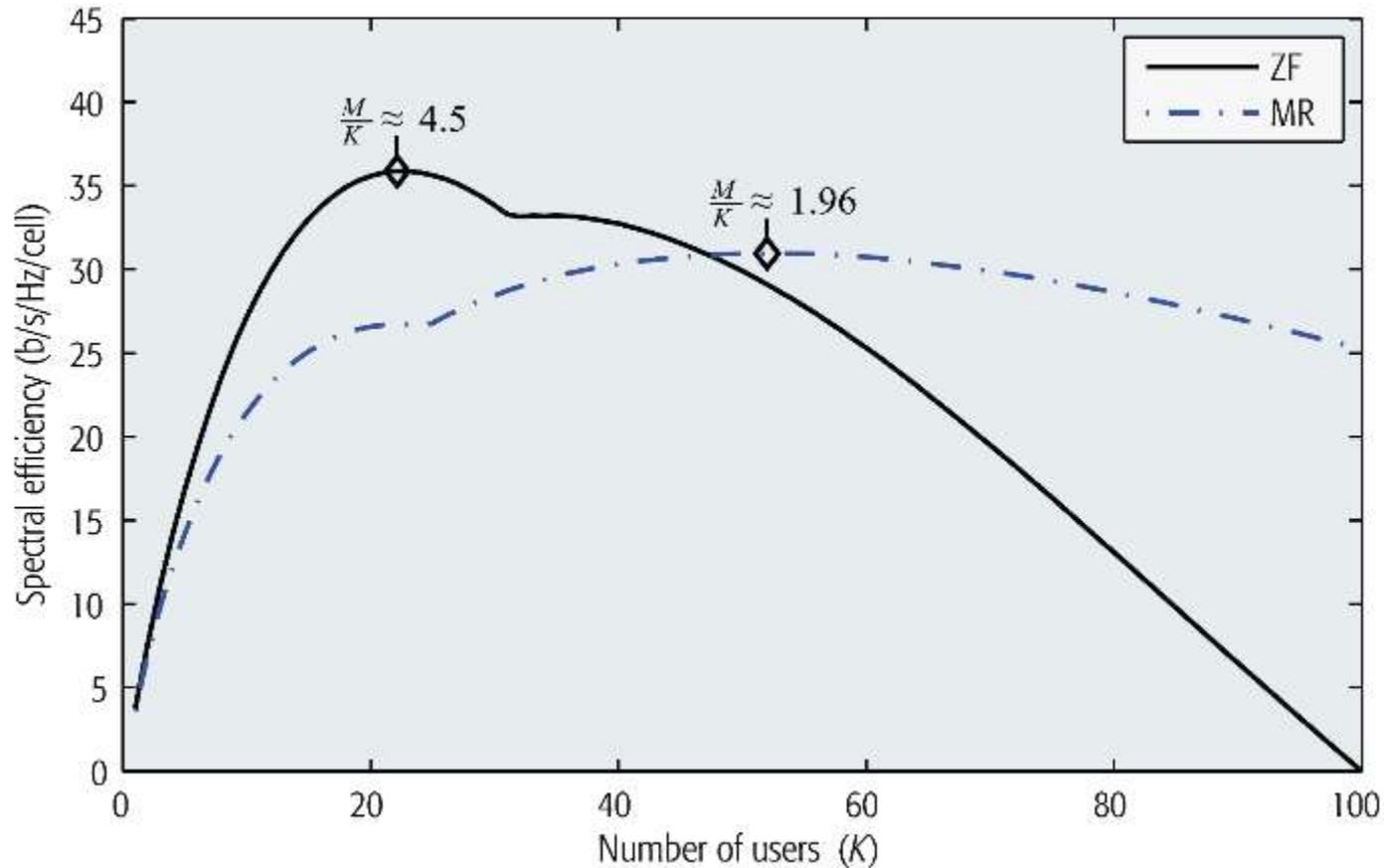
# How many users?

- Independent of # of antennas !
- Number of pilots
- Channel coherence time
- < Half of the frame (optimum rate)



- Coherence time? Small cell and indoor applications

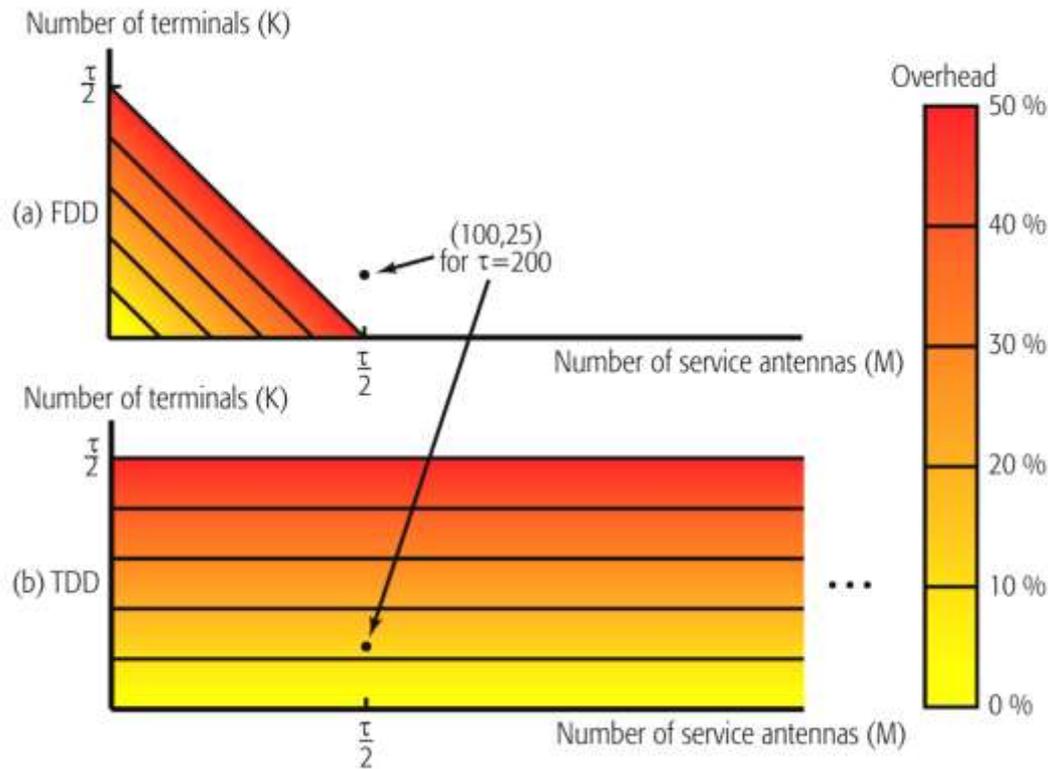
# How many users ?



M= 100  
Antennas

Emil Björnson, Erik G. Larsson, Thomas L. Marzetta, "Massive MIMO: Ten Myths and One Critical Question," IEEE Communications Magazine, vol. 54, no. 2, pp. 114-123, February 2016.

# MaMIMO in FDD



FDD only in low-mobility and low-frequency scenarios

Emil Björnson, Erik G. Larsson, Thomas L. Marzetta, "Massive MIMO: Ten Myths and One Critical Question," IEEE Communications Magazine, vol. 54, no. 2, pp. 114-123, February 2016.

# MaMIMO in FDD

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- Precoding based on partial CSI
  - Compresses Sensing
  - High correlation between antennas
  - No need for all CSI
  - Feedback only some CSI
- Channel reciprocity in FDD
  - Frequency correction algorithms
  - Based on DOA, Cov. Matrix , ...

# MaMIMO and Hetnets

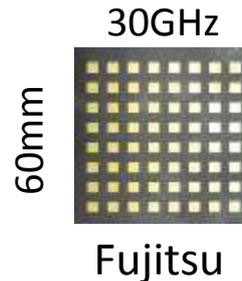
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- Hetnet
- Improving spectral efficiency
- Energy efficiency
- Interference managements between MacroBS and Small BS
- Load balancing – user association
- Massive MIMO Backhuals for small cells

# mmWave and MaMIMO

- mmWaves for massive MIMO

- Shorter distances
- Compact arrays

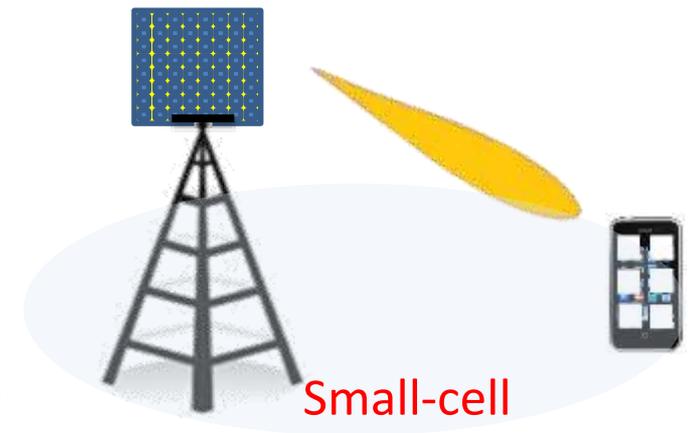


- Massive MIMO for mmWave

- Compensating the path loss - Higher range

- LOS propagation and spatial multiplexing

- Higher Doppler shift and shorter coherence time

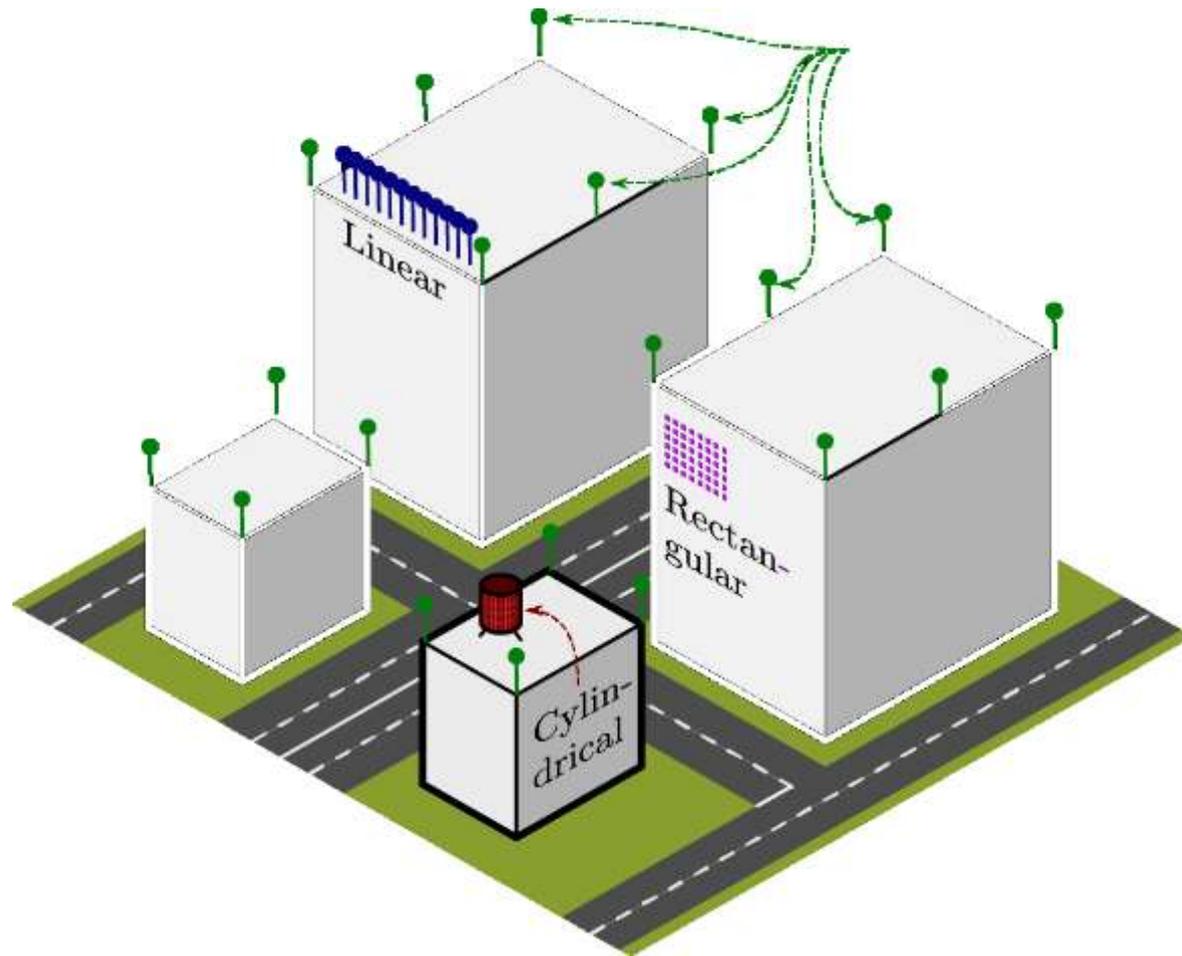


# mmWave and MaMIMO

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- mmWave is not necessary for MaMIMO
- $f=2\text{GHz}$  ( 15cm)
- 400 dual-polarized antennas  $\rightarrow$  in a 1.5 x 1.5 m array

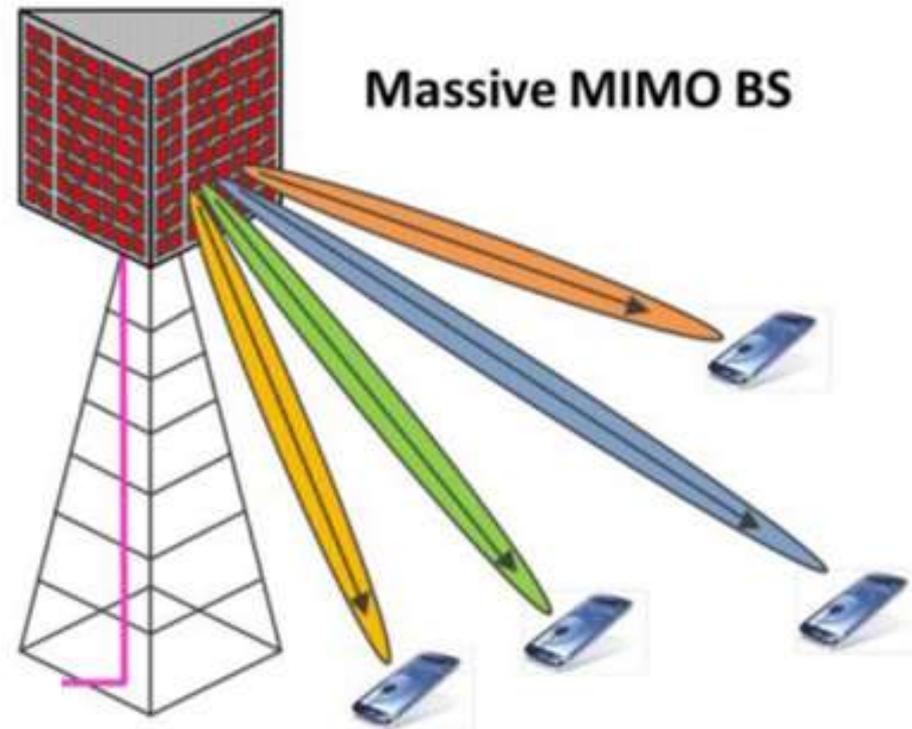
# Massive MIMO Deployment



Emil Björnson, "Massive MIMO: Bringing the Magic of Asymptotic Analysis to Wireless Networks", CAMAD, 2014

# Full dimensional-MIMO and 3D Beamforming

- Two dimensional array - FD-MIMO
- Three dimensional beam-steering (elevation & azimuth): 3DBF
- Adaptive beamforming
- 3GPP Release 13 for LTE
- Massive MIMO
  - Very narrow beams
  - No inter-user Interference



# Other Topics

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- Non-orthogonal Multiple Access (NOMA)
- Filter Banks Multi-Carriers (FBMC)
- Full Duplex Communications
- Simultaneous Wireless Power and Information Transfer (SWIPT)
- Cognitive Radio



# **Massive MIMO Implementation and Testbeds**

# Practical Challenges

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- Antenna array configuration
  - Mutual coupling
- Transceiver impairments
  - nonlinearities in amplifiers
  - Phase noise in local oscillators
  - quantization errors in analog-to-digital converters
  - I/Q imbalances in mixers
  - non-ideal analog filters

E. Bjornson *et al.*, "Massive MIMO Systems with Non-Ideal Hardware: Energy Efficiency, Estimation, and Capacity Limits," *IEEE Trans. Info. Theory*, vol. 60, no. 11, 2014.

# Practical Challenges

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- High PAPR
- Low-cost power-efficient RF amplifiers
- Coherent processing
- Reciprocity calibration

E. Björnson *et al.*, "Massive MIMO Systems with Non-Ideal Hardware: Energy Efficiency, Estimation, and Capacity Limits," *IEEE Trans. Info. Theory*, vol. 60, no. 11, 2014.

# Experimental Results

- Cylindrical or linear antenna arrays
- 128 elements array
- 2.6 GHz and 50 MHz BW



# LuMaMI

- 160 dual-polarized patch antennas – 10 UEs
- 3.7 GHz, and the element spacing is 4 cm (half a wavelength)
- TDD



# Argos

- Rice University



\$2.4 million from the  
National Science  
Foundation (NSF)

# Argos V2

- 96 Antennas (Scalable to 144 Antennas)
- TDD



C. Shepard, H. Yu, and L. Zhong, "ArgosV2: A flexible many-antenna research platform," in Proc. 2013 Annual International Conf. Mobile Comput. Netw., 2013.

# Southeast University (SEU)

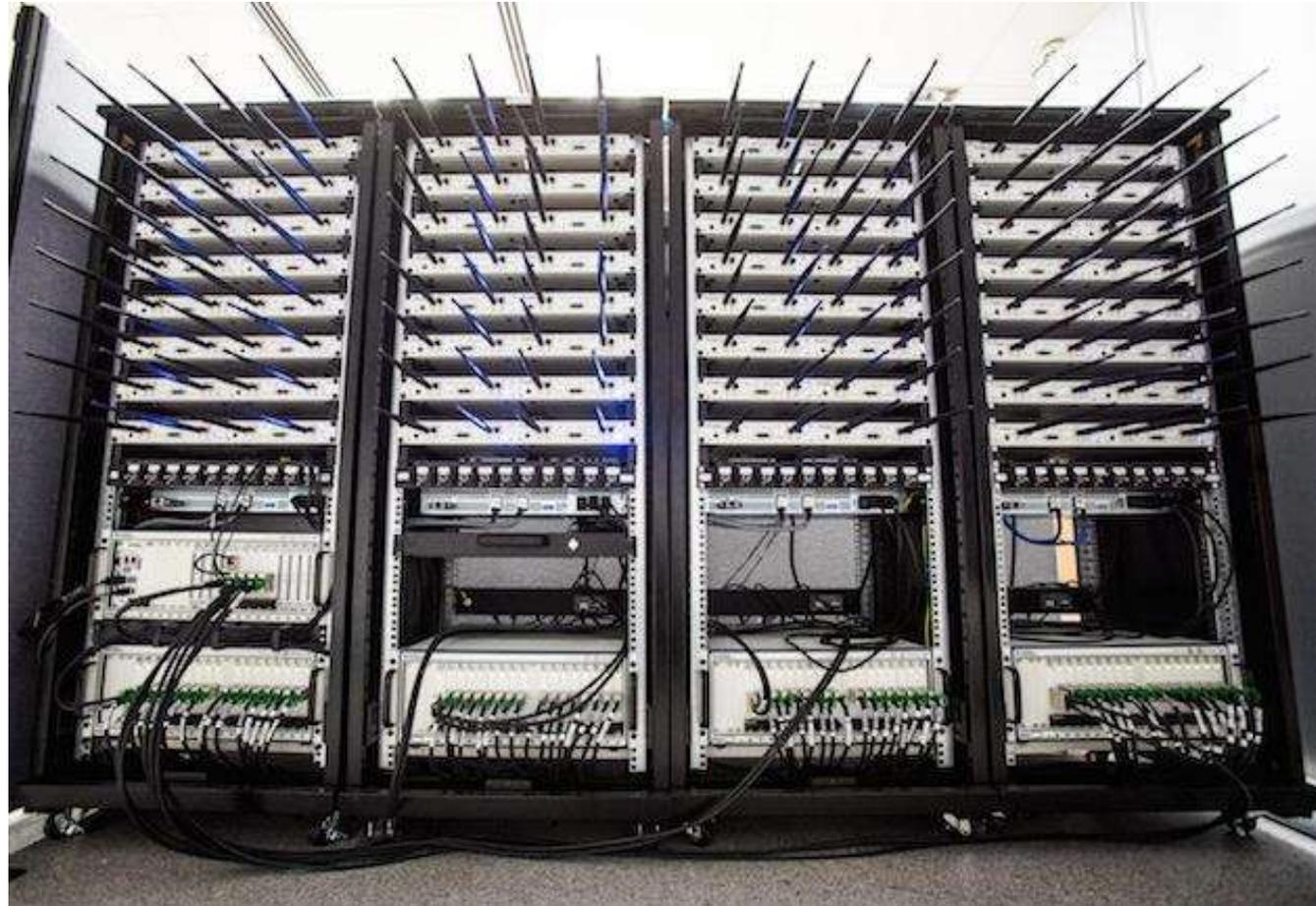
- 128 antenna base station
- 12 UEs
- 5.8 GHz
- 20 MHz
- The maximum spectral efficiency 80.64 bit/s/Hz
  - 12 single-antenna users with 256-QAM modulation
- 268.8 Mbps rate was achieved for eight single-antenna users using QPSK modulation



X. Yang , et.al. " Design and Implementation of a TDD-Based 128-Antenna Massive MIMO Prototyping System",2016

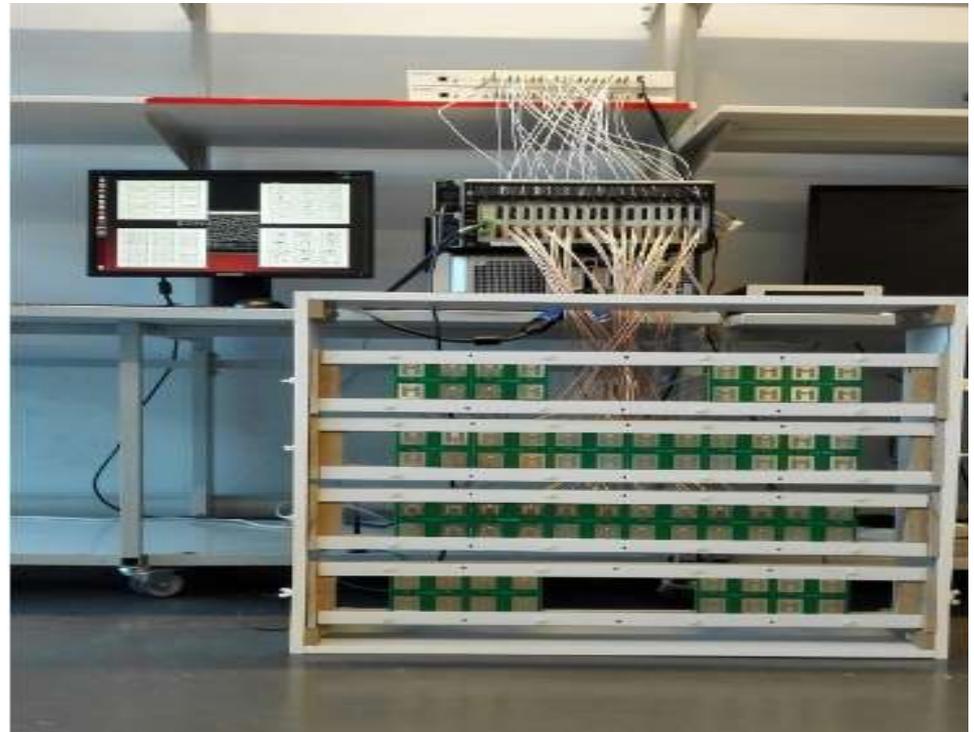
# University of Bristol

- 128-antenna
- 12 UEs
- 3.5 GHz
- 20 MHz



# OpenAirInterface Massive MIMO testbed

- Open source platform
- TDD based
- 64 elements
- 2.6GHz
- 5MHz bandwidth
- up to 4 commercial UEs



# Massive MIMO, from Nokia and Mitsubishi

- 16X16



<http://technical.ly/brooklyn/2015/04/10/wireless-future-demos-brooklyn-5g-summit/>

# Summary

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- Challenges:
- Antenna array
- 3D channel modeling
- FDD operation
- Antenna calibration
- Pilot contamination
- Hardware and implementation challenges



**Thank you**

**Questions?**

[www.mobilebroadband.ir](http://www.mobilebroadband.ir)